

1     **Development of ultra-low cycle fatigue life prediction model for structural steel considering**  
2             **the effects of surface roughness, loading frequency, and loading amplitude**

3  
4  
5     **Abstract**

6     Abrasive blast cleaning is often done for steel structures before applying various protective coatings, which  
7     produces rough surfaces with changes in fatigue properties. This problem has been addressed in the low-  
8     and high-cycle fatigue regimes; however, the effect of surface roughness in combination with different  
9     loading parameters on the ultra-low cycle fatigue (ULCF) life has not been reported thus far. To this aim,  
10    a total of 59 ULCF tests on designed specimens of SM400 steel with five levels of surface roughness were  
11    performed under various loading frequencies and displacement amplitudes. The analysis of experimental  
12    results indicates a substantial reduction in fatigue life with an increase in the surface roughness and loading  
13    amplitude and a decrease in the loading frequency. Additionally, the strength degradation, dissipation  
14    energy, and load–displacement curves are discussed in detail. With the use of experimental data, a new life  
15    prediction model characterizing the combined effects of surface roughness, loading frequency, and loading  
16    amplitude on the ULCF life is proposed. Moreover, the proposed model is validated by predicting the  
17    fatigue life under variable and constant loading amplitude patterns. Comparison between experimental and  
18    theoretical results shows that the proposed model accurately estimates the ULCF life within an error band  
19    of  $\pm 15\%$ , with a reasonable selection of model parameters.

20    **Keywords:** loading amplitude, loading frequency, life prediction, surface roughness, structural steel, ultra-  
21    low cycle fatigue

<b>Nomenclature:</b>			
$R_z$	10-point mean roughness	$N_f$	Experimental fatigue life
$R_{zr}$	Reference surface roughness	$N_r$	Reference fatigue life
$R_a$	Arithmetic mean deviation	$N_{f,p}$	Predicted fatigue life
$R_q$	Root mean squared height	$\Delta\varepsilon$	Strain range
$R_t$	Total profile height	$\Delta\varepsilon_{eq}$	Equivalent strain range
$c_1, \alpha$	Model parameters related to Coffin-Manson's relationship	$c_2, \beta$	Model parameters related to equation (5)
$c_3, \gamma$	Model parameters related to equation (8)	$c_4, \eta$	Model parameters related to equation (17)
$n_i$	Number of cycles corresponding to the $i$ th displacement range	$f$	Loading frequency
		$f_r$	Reference loading frequency
$\rho$	Radius of curvature	$R^2$	Coefficient of determination
$\varepsilon$	Evaluated strain	$z$	Surface height
$b$	Distance of neutral axis from surface	$d$	Displacement amplitude
$R$	Displacement ratio		
<b>Acronyms</b>			
ULCF	Ultra-low cycle fatigue	LCF	Low cycle fatigue
AASHTO	American Association of State Highway and Transportation Officials	ASTM	American Society for Testing and Materials
JIS	Japanese Industrial Standard	CA	Constant loading amplitude
VA	Four-step incremental loading	VB	Varying mean loading amplitude
VC	Two-step incremental loading	PE	Percentage error
APE	Average percentage error	SD	Standard deviation
RCSC	Research Council for Structural Connections	JASS	Japanese Architectural Standard Specifications
ISO	International Organization for Standardization		

24 **1 Introduction**

25 Failure of structural steel members under strong cyclic excitation was observed in steel braces, welded  
 26 beam-column connections, and steel bridge piers during the historical Kobe earthquake of 1995 and the  
 27 Northridge earthquake of 1994 (Miller, 1998; Nakashima et al., 1998; Tamura et al., 2018). In low cycle

28 fatigue (LCF), failure is characterized by crack initiation that propagates under cyclic reversals and  
29 ultimately emerges as a fracture (Xue, 2008). A phenomenon whereby enormous strain amplitudes are  
30 applied and fracture occurs after experiencing dozens to hundreds of cycles is termed ultra LCF (ULCF)  
31 (Lee et al., 2022; Wang et al., 2021). It has been investigated that when the number of loading cycles falls  
32 below approximately 200, the strain life relation may deviate from Coffin-Manson's relation because of the  
33 change in damage mechanisms (Kuroda, 2002; Nip et al., 2010; Xiang et al., 2017). Metal structures are  
34 prone to plastic deformation under strong cyclic excitations, such as destructive earthquakes. Damage to  
35 structures is associated with the unstable behavior of thin-walled members in steel braces owing to the large  
36 plastic deformations with the beginning of local buckling. When structures experience extreme earthquakes,  
37 a major part of the damage occurs within hundreds of loading cycles, which induces concentrated larger  
38 cyclic deformation with loading reversals and eventually leads to ductile fracture (Jia et al., 2014; Jia and  
39 Ge, 2018; Park et al., 2004). According to the American Association of State Highway and Transportation  
40 Officials (AASHTO, 2012) LRFD bridge design specifications, investigation entirely based on inelastic  
41 modeling may be required for limit states in case of extreme events. Therefore, considering the ULCF  
42 fracture as a limit state for the seismic design of steel structures is suggested.

43 The LCF life of structural steel has been comprehensively studied by considering the parameters of strain  
44 range, loading frequency, and temperature, and can be predicted using the Coffin–Manson relationship (L.  
45 F. Coffin, 1954). Recently, researchers have proposed modified Coffin–Manson models to improve the life  
46 prediction accuracy in the ULCF regime. Tateishi et al., (2007) established a prediction model in an  
47 extremely LCF regime by introducing the concept of damage mechanics under variable loading amplitude.  
48 Ge and Kang (2012) proposed a damage index for evaluating ductile crack initiation in steel members by  
49 combining Miner's rule (Miner, 1945) and Coffin–Manson model and validated this index for steel bridge  
50 piers. Xue (2008) established a unified expression for the prediction of LCF and ULCF life using material  
51 parameters and an exponential function. Li et al., (2020) modified the Coffin–Manson model by including

52 the effects of stress triaxiality for the prediction of ULCF fracture in steel. Through this model, empirical  
53 relations were established between stress triaxiality and model parameters. Tamura et al., (2009) explored  
54 the effect of stress triaxiality on brittle fractures in steel bridge bents under severe earthquakes. A  
55 deformation history-based approach for damage evaluation of steel members under the ULCF regime was  
56 also adopted (Xie et al., 2020). This model could predict fatigue life from the displacement history of  
57 structures with the application of Miner's rule and life curves. Moreover, a prediction model considering  
58 the buckling effect was proposed for investigating ductile fracture in bracing members under an extremely  
59 LCF regime (Xu et al., 2020). This model was efficient for predicting the initiation and propagation of  
60 fracture by incorporating the effects of stress triaxiality and load angle. Salawdeh and Goggins (2013)  
61 incorporated a fatigue model to steel brace members for predicting their structural performance under cyclic  
62 loading. Moreover, seismic loading includes both cyclic and dynamic characteristics (Wang et al., 2021),  
63 and actual structures also respond to extreme earthquakes in a dynamic manner. However, the discussed  
64 models were based only on large strain amplitudes and ignored the parameter of loading frequency. Hence,  
65 incorporating and investigating the effect of frequency on the ULCF life of structural steel are required.

66 During earthquakes, steel structures in local areas endure both large strain and high frequency loading  
67 (Tamura et al., 2012) and existing studies have explored the effects of loading rate on their LCF life. Luo  
68 et al., (2013) investigated the effects of frequency from 0.001 to 3 Hz subjected to constant strain amplitude  
69 and observed an increase in fatigue life with the frequency until a transition strain rate value of 0.01 /sec  
70 after which the phenomenon reversed. Another study by Kanchanomai et al., (2003) developed a frequency  
71 modified Coffin–Manson relationship for a eutectic solder and observed that the fatigue ductility coefficient  
72 was highly influenced by the loading frequency ranging from 0.001 to 1 Hz. Reddy, et al., (2015a, 2015b)  
73 studied the effect of strain rate in combination with varying nitrogen content on the substructural changes  
74 and cyclic deformation occurring in 316LN stainless steel and found the predominance of thermal recovery  
75 over dynamic strain aging. For illustrating the order of loading rate under earthquake, existing studies

76 asserted the possibility of strain rate increasing to approximately 1.0 /sec during an earthquake,  
77 corresponding to a loading frequency of 5 Hz at the local areas of steel bridge piers during the earthquake  
78 of 1995 (Sinsamutpadung et al., 2016; Sinsamutpadung and Sasaki, 2018), while another study by Tamura  
79 et al., (2012) also highlighted the possibility of strain rate reaching approximately 1.5 /sec in P75 steel  
80 bridge pier under cyclic loading. However, all these investigations were conducted in the LCF region. To  
81 create a realistic condition of extreme earthquakes in the ULCF regime, the parameters of strain amplitude  
82 and loading rates covering quasi-static to dynamic conditions should be considered. Therefore, all the  
83 experiments conducted for this study were configured to replicate these conditions.

84 Usually, metal structures including steel bridges undergo abrasive blasting treatment to rough the surface  
85 of substrates before the application of adhesive coatings to remove corrosion, dirt, grease, scratches, or any  
86 foreign material. Although the treatment assures a better coating adhesion, it reduces the service life of the  
87 structures (FHWA, 2015; Kainuma, 2021; NILIM, 2020). Researchers have observed a significant impact  
88 of surface roughness on the fatigue life of steel subjected to cyclic loading. Generally, fatigue cracks  
89 originate from the surface (Hasunuma et al., 2019); thus, the parameter of roughness cannot be neglected  
90 in real engineering practices. The extent of surface roughness causes high strain concentration, lowers the  
91 capacity to resist fatigue damage, and ultimately reduces the fatigue life of materials (Wang et al., 2017).  
92 Pegues et al., (2018) analyzed the size and effect of surface roughness on a high cycle fatigue regime by  
93 designing a number of additively manufactured Ti-6Al-4V specimens and concluded that the fatigue life  
94 was more sensitive to bar diameter than to the surface area. Wang et al., (2016) developed the Giga-fatigue  
95 life prediction model by employing energy theory to investigate the fracture development in FV520B-I  
96 steel, taking surface roughness as the primary variable. In addition to the experimental research, Singh et  
97 al., (2019) adopted a microstructure-based approach for modeling the impact of surface roughness on tensile  
98 fatigue. Average roughness was measured by optical surface profilometry and reduction in fatigue strength  
99 with an increase in surface roughness was predicted. Wang et al., (2013) studied the evolution of surface

100 roughness in 316L stainless steel under LCF and indicated that an increase in surface roughness at early  
101 fatigue life and slip band formation were the main causes of the phenomenon. Some studies investigated  
102 the effect of blasting on fatigue life. Poorna Chander et al., (2009) grit blasted steel substrates using alumina  
103 of several sizes by varying time, angle, pressure, and stand-off distance to check their effect on surface  
104 roughness. They observed an increase in the subsurface hardness and residual stress with the considered  
105 parameters. McKelvey and Fatemi (2012) checked the fatigue life of forged steel and developed life curves  
106 as a function of hardness based on their experimental findings. Song et al., (2021a, 2021b) investigated the  
107 ULCF properties and fracture process of corroded steel and found that fatigue life is significantly reduced  
108 by the increasing level of surface roughness induced by the corrosion process. Additionally, processing  
109 parameters are known to have a strong impact on fatigue life, and variation in surface morphology largely  
110 affects the LCF life (Hasunuma et al., 2019). Thus, investigating the effect of surface roughness, produced  
111 by blasting, on the ULCF life is important. Considering the literature, the existing models evidently lack  
112 the ability to investigate the fatigue failure induced by surface roughness for structural steel. Moreover, the  
113 parameters of surface roughness in combination with loading frequency and loading amplitudes are  
114 important and should not be neglected during the model development of metals in the ULCF regime.

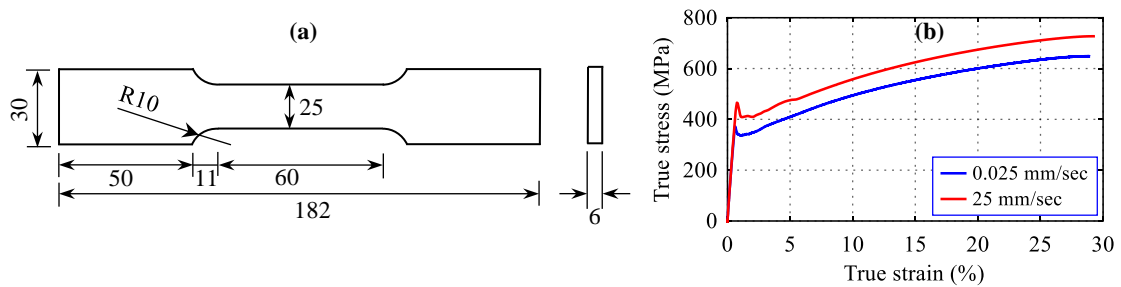
115 Thus far, no consensus has been achieved on investigating the combined effects of surface roughness,  
116 loading frequency, and loading amplitude on the ULCF life of structural steel. Thus, this study focuses on  
117 the development of a new ULCF life prediction model by conducting a total of 59 displacement controlled  
118 ULCF tests on notched steel specimens with different surface roughness. The load response, dissipated  
119 energy response, and load–displacement curves of the ULCF tests for processed specimens under different  
120 loading frequencies and loading amplitudes are analyzed through focused experimentation. A laser  
121 scanning technique was used to find the strain directly during the experiment by using the radius of  
122 curvature. Based on the experimental data, a new ULCF life prediction model with surface roughness  
123 coupling the effects of loading frequency and loading amplitude is proposed. Constant amplitude test results

124 are utilized for calibrating the model parameters by performing regression analysis. Lastly, the proposed  
 125 method is verified by the comparison of experimental and predicted fatigue life under constant and variable  
 126 loading amplitude tests. The presented simplified model is a first of its kind as it combines all model  
 127 parameters related to surface roughness, loading frequency, and loading amplitude and is expected to find  
 128 application in improving the design guidelines for steel structures subjected to extreme loading conditions.

## 129 2 Experimental program

### 130 2.1 Material and test specimens

131 All considered specimens were composed of mild steel plate JIS-SM400 (JIS G 3106, 2004) equivalent to  
 132 ASTM A283 (American Society for Testing and Materials), which is a broadly used steel for the  
 133 construction of welded structures in Japan. Monotonic tensile tests at the quasi-static and dynamic  
 134 displacement rates of 0.025 and 25 mm/sec, respectively, were performed on coupon specimens for  
 135 obtaining the mechanical properties of the test material. Figure 1(a) illustrates the specimen geometry, while  
 136 the chemical composition and material properties of SM400 steel are summarized in Table 1. The true  
 137 stress–strain curves attained from the tension test at different displacement rates are shown in Figure 1(b).



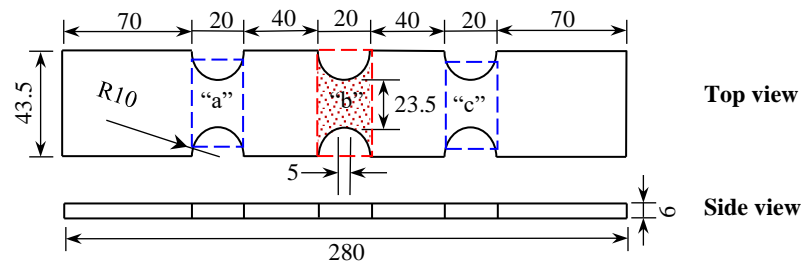
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139 **Figure 1.** Tensile Test (a) Configuration of coupons for the tensile test (dimensions are in units of mm) (b)  
 140 Comparative true stress–strain relationships

141 **Table 1.** Mechanical and chemical properties of SM400 steel

Test steel	Disp. rate (mm/sec)	Yield stress (MPa)	Tensile stress (MPa)	Chemical composition (% wt)				
				C	Si	Mn	P	S
SM400	0.025	372	649	0.15	0.22	0.84	0.019	0.007
	25	462	727					

142 For investigating the behavior of structural steel under various loading conditions, uniaxial fatigue tests  
 143 were conducted on double-edge notched steel specimens, shown in Figure 2. All tension and fatigue test  
 144 specimens were prepared from the same 6 mm thick SM400 steel plate. Since surface blasting was  
 145 performed at the central region of  $20 \times 43.5 \text{ mm}^2$  (region “b”), applying a large strain amplitude at the same  
 146 location for fracture occurrence was necessary. For achieving this goal, semicircular notches of radius 10  
 147 mm were formed in regions “a, b, and c”. After load application, plastic hinges were developed in regions  
 148 “a and c”, while a large strain was developed in observation region “b”. A moderate notch radius was  
 149 chosen to prevent the uncertainty of crack and fracture formations outside the observation region and  
 150 maintain a constant buckling length. Moreover, the specimen length was kept at 280 mm for producing the  
 151 buckling phenomenon. Briefly, the experimental method was established in such a way that ① a large  
 152 amplitude cyclic loading was generated at the central region “b” using buckling deformation of the  
 153 specimens (Tateishi et al., 2007), ② the deformation was concentrated at region “b” of the specimens  
 154 through side notches and ③ strain from the central region curvature was directly evaluated in a non-contact  
 155 manner by laser scanning (Saleem et al., 2022). Since the curvature of steel specimens was concentrated at  
 156 their center, the location of the fracture was localized. The specimens were designed to simulate the local  
 157 buckling behavior of steel members i.e., steel plates, and steel braces for clarifying failure under ULCF  
 158 loading (Park et al., 2004; Tateishi et al., 2007).



159  
 160 **Figure 2.** Geometry of specimens for fatigue tests (dimensions are in units of mm), where “b” is the  
 161 region of surface treatment



162 **2.2 Introduction and measurement of surface roughness**

163 As per the International Organization for Standardization (ISO 8501, 2007; ISO 8503-1, 2012) guidelines,  
164 abrasive blasting is usually done on metal surfaces for the application of paint and other protective coatings.  
165 During the process, rust, mill scale, and other unwanted contaminants are removed from the surface. Thus,  
166 abrasive blasting with different surface roughness can significantly affect fatigue strength. To investigate  
167 the effect of surface roughness on ULCF life, flat surfaces of steel specimens were blasted to achieve 10-  
168 point mean roughness  $R_z$  of five different levels 20, 40, 60, 80, and 100  $\mu\text{m}$  in this study. In Japanese  
169 Industrial Standard (JIS B 0601, 2013), rough profiles are represented by parameter  $R_z$  because it is more  
170 sensitive to occasional deep valleys or high peaks than arithmetic mean roughness  $R_a$ ; hence, the roughness  
171 was indicated by the parameter  $R_z$ . The recommended values of the surface roughness  $R_z$  for blast-cleaned  
172 steel surfaces range from 25 to 80  $\mu\text{m}$ , with a maximum value of 100  $\mu\text{m}$ , according to ISO 8503-1, (2012).  
173 The Japanese Architectural Standard Specification (JASS 6, 2007) recommends carrying out the surface  
174 blasting treatment resulting in surface roughness of less than 100  $\mu\text{m}$  for steel metal cut surfaces and surface  
175 roughness  $R_z$  of larger than 50  $\mu\text{m}$  in case of high strength bolted connections to achieve the friction  
176 coefficient of 0.45 (Nakajima et al., 2011). Moreover, for thermally cut holes of bolted connections which  
177 are explicitly allowed in buildings, the surface roughness should not exceed 25  $\mu\text{m}$  as per the Research  
178 Council on Structural Connections (RCSC, 2020) guidelines. So, the surface roughness levels of abrasive  
179 surfaces employed in this study were selected accordingly. Since the goal of this study is to evaluate the  
180 effect of fine to rough surfaces, combined with other loading parameters, on the ULCF life of structural  
181 steel, so by using different combinations of machining parameters, such as abrasive type, shape, and size;  
182 blasting pressure; and nozzle distance, five different values of  $R_z$ , ranging from 20 to 100  $\mu\text{m}$ , were  
183 obtained. The adopted machining parameters and conditions for abrasive blasting are listed in Table 2.  
184 The surface roughness of the specimens was measured with a roughness measuring device, SurfTest SV-  
185 2000 (Mitutoyo, Japan) that provides a two-dimensional (2D) surface profile. Measurements were

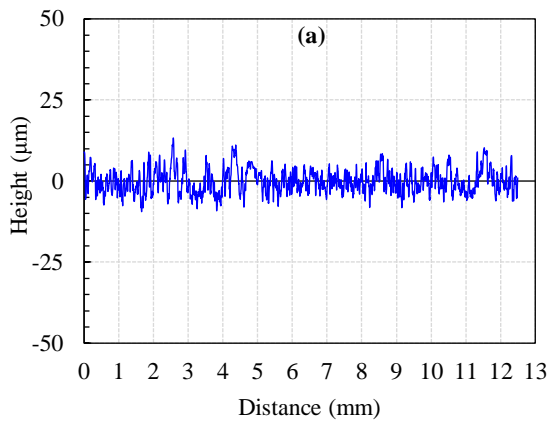
186 conducted using a tip radius of 2  $\mu\text{m}$ , range of 800  $\mu\text{m}$ , measurement pitch of 0.001  $\mu\text{m}$ , and lower and  
 187 upper cut-off wavelengths of 0.008 and 2.5 mm, respectively. The representative 2D roughness profiles  
 188 along the longitudinal direction (y-direction in Figure 17) for five different cases are illustrated in Figure 3.  
 189 These surface textures were measured over a length of 12.5 mm with repetitions at different locations.  
 190 Table 3 presents the mean values of the measured  $R_z$  (10-point height),  $R_a$  (arithmetic mean deviation),  $R_q$   
 191 (root mean squared height), and  $R_t$  (total height) for a population of 10 samples for each surface condition.

192 **Table 2.** Machining parameters adopted to achieve the targeted surface roughness  $R_z$

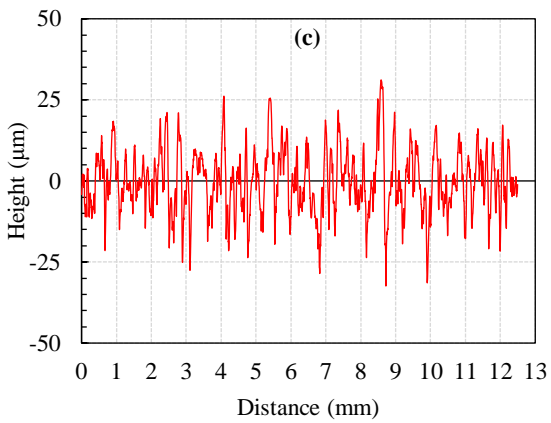
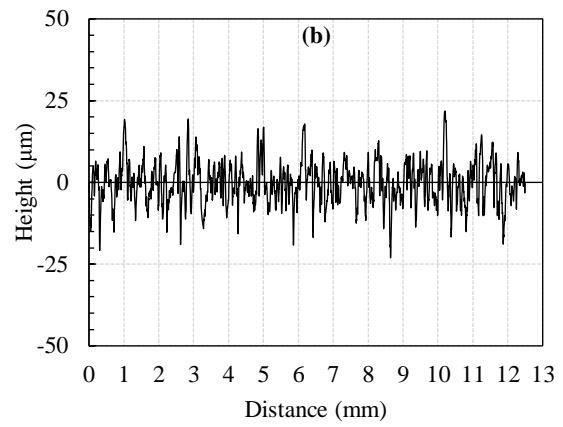
Machining parameters	Targeted surface roughness, $R_z$ ( $\mu\text{m}$ )				
	20	40	60	80	100
Abrasive material	Alumina (A-80)	Alumina (A-36)	Alumina (A-24)	Steel grid (G-120H)	Steel grid (G-120H)
Shape of abrasive	Sharp grains	Sharp grains	Sharp grains	Sharp grains	Sharp grains
Size of abrasive	~ 0.2 mm	~ 0.5 mm	~ 0.7 mm	~ 1.2 mm	~ 1.2 mm
Blasting pressure	0.45MPa	0.50MPa	0.45MPa	0.17MPa	0.38MPa
Equipment used	SAM-6	SAM-6	SAM-6	DM-8 (AT-20)	DM-8 (AT-20)
Blasting angle	~ 90°	~ 90°	~ 90°	~ 90°	~ 90°
Blasting distance	~ 100 mm	~ 100 mm	~ 100 mm	~ 150 mm	~ 150 mm

193 **Table 3.** Mean values of evaluated roughness parameters for each surface condition

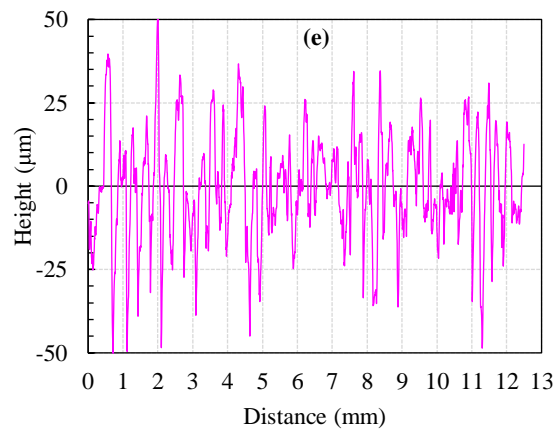
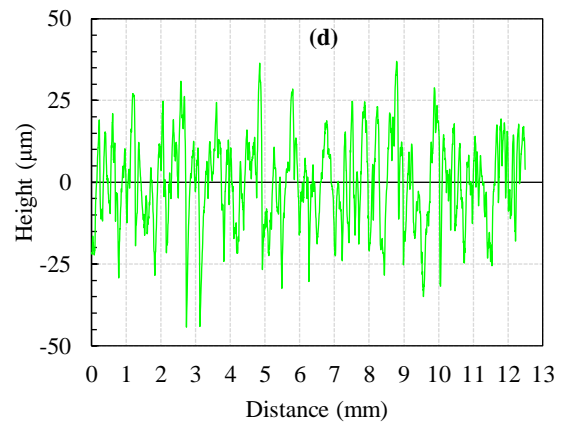
Roughness parameters ( $\mu\text{m}$ )	Targeted surface roughness, $R_z$ ( $\mu\text{m}$ )				
	20	40	60	80	100
$R_z$	17.69	38.43	61.65	77.16	96.16
$R_a$	2.98	4.98	8.1	10.21	14.42
$R_q$	3.64	6.34	10.49	13.47	18.48
$R_t$	22.76	44.94	71.11	107.74	123.75



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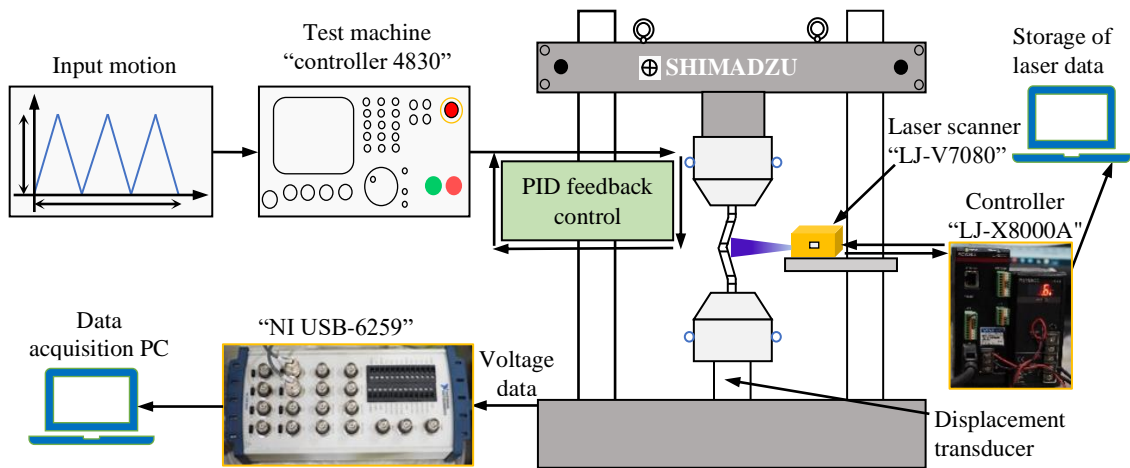
197 **Figure 3.** 2D surface roughness profiles for (a) 20, (b) 40, (c) 60, (d) 80, and (e) 100  $\mu\text{m}$

198 **2.3 Fatigue experiment setup and procedure**

199 A total of 59 ULCF tests were performed on notched steel specimens with variable surface roughness  
200 subjected to various loading conditions. A displacement-controlled cyclic loading protocol with a  
201 displacement ratio  $R = d_{\min}/d_{\max} = 0$ , having a triangular waveform, was used to ascertain the process  
202 of ULCF fracture formation. Tests were performed at room temperature employing an electrohydraulic  
203 servo testing machine (EHF-EV200kN, Shimadzu, Japan) with a loading capacity of 200 kN. The  
204 experimental testing system is shown in Figure 4. The top end of the test specimen was fixed, while the  
205 bottom end was free in the longitudinal direction. The rotational degrees of freedom along the longitudinal  
206 direction at the bottom were free, while the other two rotational degrees of freedom were fixed. The  
207 feedback to control the input displacement was obtained from the displacement transducer attached to the  
208 actuator of the machine. A default displacement transducer was built into the actuator of the machine. In  
209 this study, PID (proportional–integral–derivative) control, a fully digital and non-linear feedback control  
210 algorithm, was implemented for measuring the exact displacement and applying a high frequency loading.  
211 In addition to the algorithm, a laser scanner (KEYENCE, LJ-V7080) with a measurement pitch of 50  $\mu\text{m}$   
212 was oriented perpendicular to the center of the specimen for measuring the surface topography of the  
213 observation region, from which the strain value was directly calculated.

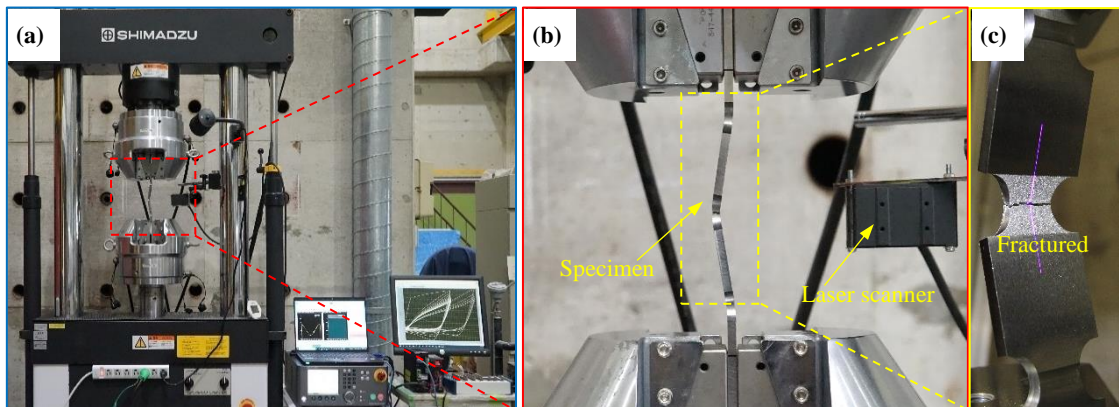
214 According to ASTM E1049-85 (2011) guidelines stating the procedure for cycle counting in fatigue  
215 analysis,  $N_f$  can be taken as the number of loading cycles that a specimen could sustain before the failure  
216 of a particular nature occurred. The loading continued until the initiation of specimen fracture, and  $N_f$  was  
217 determined corresponding to the abrupt change in the slope of load–displacement curve under tensile  
218 loading cycle (Li et al., 2021; Tian et al., 2021; Xie et al., 2020). Figure 5 shows an image of the actual  
219 specimen subjected to the fatigue test. Fracture took place across the locally buckled area at the mid-height  
220 of the specimen when it was stretched under tensile loading.

221



222

223 **Figure 4.** Schematic of experimental system and signal flow



224

225 **Figure 5.** (a) Actual specimen setup and devices used during the experiment (b) Lateral and local buckling

226 (c) Fracture across the locally buckled area at the mid-height of the specimen

## 227 2.4 Grouping of experimental fatigue specimens and loading conditions

228 To investigate the combined effects of surface roughness, loading amplitude, and loading frequency on the

229 ULCF life of steel, 11 types of loading conditions were selected for each roughness case, and a total of 55

230 experiments under different surface roughness were conducted. Moreover, four additional tests were also

231 performed on plain specimens to check the effect of blasting on fatigue life for comparison. The results are

232 compiled and listed in Table 4. All the notations are listed in the notes at the end of Table 7. Since the  
 233 characteristics of an extreme earthquake include fatigue failure under a smaller number of loading cycles  
 234 of high amplitude and quasi-static to dynamic loading conditions, all experiments of this study were  
 235 configured to replicate the characteristics. Test specimens were divided into three groups. The input loading  
 236 conditions along with the fatigue test results are enlisted in Tables 5, 6, and 7. The test results of the first  
 237 two groups (Tables 5 and 6) were used for the development/calibration of the proposed model, while the  
 238 results of the third group (Table 7) were used for validating the proposed model. Since the measured  $R_z$   
 239 values of the blasted specimens were not the same as the targeted values, for convenience, the targeted  
 240 roughness values were used in this study.

241 **Table 4.** Fatigue experiment results for plain specimens under constant loading amplitude

Specimen ID	$R_z$	$d$	$f$	$\Delta\varepsilon$	$N_f$
NB-CA2-0.005-Tri	No	2	0.005	0.035	153.5
NB-CA3-0.005-Tri	No	3	0.005	0.05	85.5
NB-CA4-0.005-Tri	No	4	0.005	0.065	54.5
NB-CA5-0.005-Tri	No	5	0.005	0.08	33.5

242 For the first group, constant loading amplitude (CA) tests were conducted on blasted specimens with five  
 243 levels of surface roughness. The experimental scheme and the test results are presented in Table 5.  
 244 Comparison of these results with those of plain specimens indicated that the fatigue life of blasted  
 245 specimens with 100  $\mu\text{m}$  roughness decreased by 1.8 times than those of plain specimens, revealing the  
 246 prime effect of surface roughness on the ULCF life of metal structures. The effect was more substantial for  
 247 higher values of surface roughness. This observation was explained by the presence of surface defects in  
 248 blasted specimens, which was responsible for the reduction in fatigue strength. For ULCF fracture to occur,  
 249 the amplitude of the input loading should exceed the yielding point and a large plastic deformation should  
 250 occur at the local areas of the steel member. Therefore, a number of trial tests were done to find the  
 251 amplitudes of input displacement, such that the specimen failure occurred within dozens to hundreds of

252 loading cycles. Constant amplitude tests were conducted at displacement amplitudes of 2, 3, 4, and 5 mm  
 253 under a constant loading frequency of 0.005 Hz. Since constant loading amplitude is the standard testing  
 254 protocol used to characterize fatigue properties, the results of the tests were used for the calculation of  
 255 material constants and calibration of the proposed model.

256 **Table 5.** Fatigue experiment results for blasted specimens under various constant loading amplitudes

Specimen ID	$R_z$	$d$	$f$	$\Delta\varepsilon$	$N_f$	$N_{f,p}$
B20-CA2-0.005-Tri	20	2	0.005	0.035	148.5	129.42
B20-CA3-0.005-Tri	20	3	0.005	0.05	77.5	69.22
B20-CA4-0.005-Tri	20	4	0.005	0.065	46.5	43.69
B20-CA5-0.005-Tri	20	5	0.005	0.08	33.5	30.35
B40-CA2-0.005-Tri	40	2	0.005	0.035	113.5	105.12
B40-CA3-0.005-Tri	40	3	0.005	0.05	66.5	56.23
B40-CA4-0.005-Tri	40	4	0.005	0.065	40.5	35.49
B40-CA5-0.005-Tri	40	5	0.005	0.08	25.5	24.65
B60-CA2-0.005-Tri	60	2	0.005	0.035	108.5	93.08
B60-CA3-0.005-Tri	60	3	0.005	0.05	59.5	49.79
B60-CA4-0.005-Tri	60	4	0.005	0.065	37.5	31.42
B60-CA5-0.005-Tri	60	5	0.005	0.08	24.5	21.83
B80-CA2-0.005-Tri	80	2	0.005	0.035	97.5	85.39
B80-CA3-0.005-Tri	80	3	0.005	0.05	50.5	45.67
B80-CA4-0.005-Tri	80	4	0.005	0.065	30.5	28.82
B80-CA5-0.005-Tri	80	5	0.005	0.08	23.5	20.02
B100-CA2-0.005-Tri	100	2	0.005	0.035	78.5	79.86
B100-CA3-0.005-Tri	100	3	0.005	0.05	48.5	42.71
B100-CA4-0.005-Tri	100	4	0.005	0.065	28.5	26.96
B100-CA5-0.005-Tri	100	5	0.005	0.08	18.5	18.73

257 For the second group, ULCF tests were conducted on blasted specimens under a wide range of loading  
 258 frequencies from 0.005 to 5 Hz (Sinsamutpadung and Sasaki, 2018; Tamura et al., 2012), at an amplitude  
 259 of 5 mm, for examining their combined effect on ULCF life. The test results are shown in Table 6. The

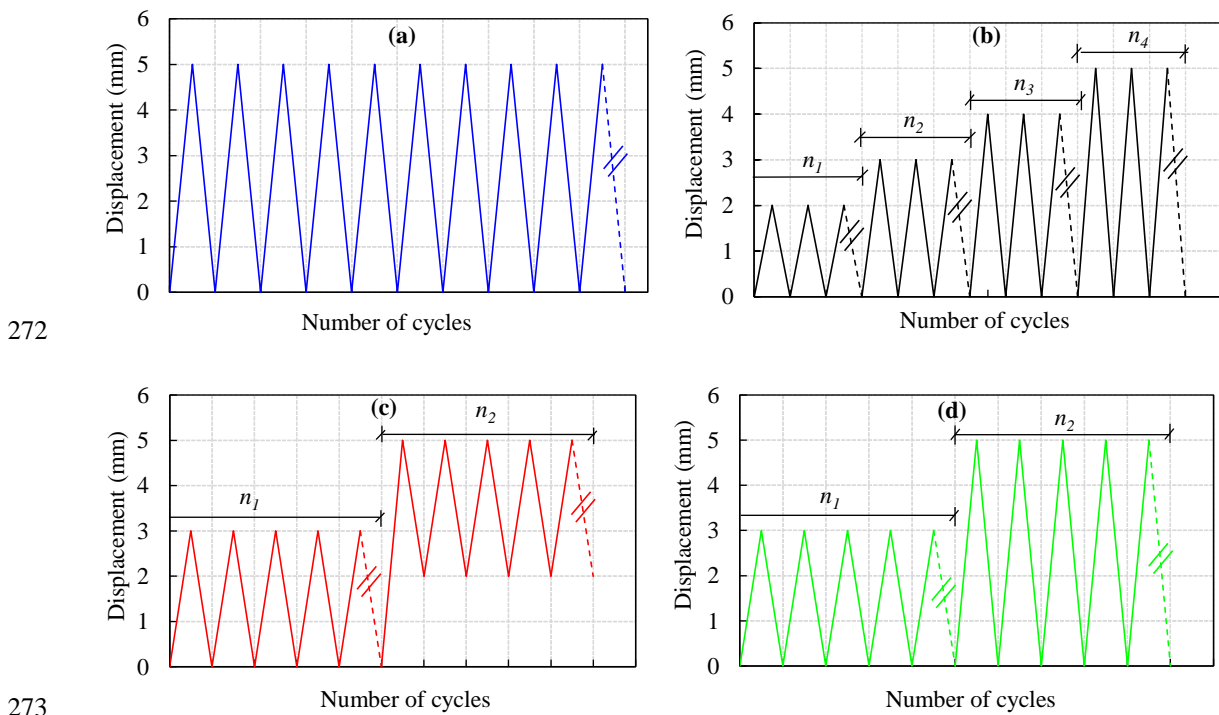
260 selected frequencies covered a wide range of displacement rates, from 0.025 to 25 mm/sec, targeting the  
 261 quasi-static to dynamic conditions of earthquakes. Since a majority of the available researchers conducted  
 262 fatigue tests at quasi-static conditions, which hardly affected the fatigue performance (Li et al., 2020; Xie  
 263 et al., 2020; Xu et al., 2020), the aforementioned frequencies were selected to simulate a real earthquake  
 264 phenomenon, with a wide range of loading frequency. Moreover, while conducting experiments at high  
 265 loading frequencies, testing was temporarily paused for approximately 1 min after the application of each  
 266 loading cycle in order to avoid the effect of temperature rise.

267 **Table 6.** Fatigue experiment results for blasted specimens under various loading frequencies

Specimen ID	$R_z$	$d$	$f$	$N_f$	$N_{f,p}$
B20-CA5-0.005-Tri	20	5	0.005	33.5	30.35
B20-CA5-0.05-Tri	20	5	0.05	35.5	32.90
B20-CA5-0.5-Tri	20	5	0.5	38.5	35.66
B20-CA5-5-Tri	20	5	5	44.5	38.65
B40-CA5-0.005-Tri	40	5	0.005	25.5	24.65
B40-CA5-0.05-Tri	40	5	0.05	27.5	26.72
B40-CA5-0.5-Tri	40	5	0.5	29.5	28.97
B40-CA5-5-Tri	40	5	5	33.5	31.40
B60-CA5-0.005-Tri	60	5	0.005	24.5	21.83
B60-CA5-0.05-Tri	60	5	0.05	25.5	23.66
B60-CA5-0.5-Tri	60	5	0.5	28.5	25.65
B60-CA5-5-Tri	60	5	5	30.5	27.80
B80-CA5-0.005-Tri	80	5	0.005	23.5	20.02
B80-CA5-0.05-Tri	80	5	0.05	24.5	21.70
B80-CA5-0.5-Tri	80	5	0.5	25.5	23.53
B80-CA5-5-Tri	80	5	5	29.5	25.50
B100-CA5-0.005-Tri	100	5	0.005	18.5	18.73
B100-CA5-0.05-Tri	100	5	0.05	20.5	20.30
B100-CA5-0.5-Tri	100	5	0.5	20.5	22.00
B100-CA5-5-Tri	100	5	5	23.5	23.85



268 For the third group, blasted specimens were tested under different variable-amplitude-loading patterns for  
 269 verifying the accuracy of the proposed model. Since actual structural members are also subjected to varying  
 270 loading amplitude apart from constant loading amplitude, three different loading patterns that replicated  
 271 seismic loading to a certain level were employed for this study as shown in Figure 6.



274 **Figure 6.** Loading patterns for test steel specimens. (a) CA, (b) VA, (c) VB, and (d) VC loading

275 The test results for this group are presented in Table 7. The loading pattern (VA) was a four-step incremental  
 276 loading with imposed displacement amplitudes of 2, 3, 4, and 5 mm. This pattern was intended to simulate  
 277 near field earthquakes causing large plastic deformations. The number of cycles in the first three steps with  
 278 amplitudes of 2, 3, and 4 mm was calculated by taking 17% of  $N_f$ , obtained from constant amplitude tests  
 279 performed at the respective amplitudes for a specific roughness case. The last step of amplitude 5 mm  
 280 continued until the specimens fractured. The loading pattern (VB) was selected to study the shift in mean  
 281 displacement amplitude and compare its fatigue life with the results of the 3 mm constant amplitude loading

282 test. In this pattern, an amplitude of 3 mm was applied by shifting the mean position of the pattern. The  
 283 number of cycles at the amplitude of 3 mm was calculated by taking 50% of  $N_f$ , obtained from constant  
 284 amplitude tests performed at the respective displacement amplitude. After shifting the mean position, the  
 285 second loading step of amplitude 3 mm continued until the specimen fractured. The loading pattern (VC)  
 286 was a two-step incremental loading pattern with imposed amplitudes of 3 and 5 mm. This pattern was  
 287 applied to investigate the effect of load sequence on fatigue life. The calculation for the number of cycles  
 288 was the same as that for pattern VB, without any shift in mean displacement after the first loading step.

289 **Table 7.** Fatigue experiment results for blasted specimens under variable loading amplitudes

Specimen ID	$R_z$	Patterns	$n_i$	$f$	$\Delta\varepsilon_{eq}$	$N_f$	$N_{f,p}$
B20-VA-0.005-Tri	20	VA	25, 13, 8, 7.5	0.005	0.0516	53.5	65.50
B20-VB-0.005-Tri	20	VB	39, 24.5	0.005	0.05	63.5	69.22
B20-VC-0.005-Tri	20	VC	39, 10.5	0.005	0.0574	49.5	54.34
B40-VA-0.005-Tri	40	VA	19, 11, 7, 5.5	0.005	0.0517	42.5	53.02
B40-VB-0.005-Tri	40	VB	33, 17.5	0.005	0.05	50.5	56.23
B40-VC-0.005-Tri	40	VC	33, 8.5	0.005	0.0572	41.5	44.41
B60-VA-0.005-Tri	60	VA	19, 10, 6, 4.5	0.005	0.0504	39.5	49.10
B60-VB-0.005-Tri	60	VB	30, 12.5	0.005	0.05	42.5	49.79
B60-VC-0.005-Tri	60	VC	30, 8.5	0.005	0.0577	38.5	38.72
B80-VA-0.005-Tri	80	VA	18, 9, 5, 4.5	0.005	0.0503	36.5	45.19
B80-VB-0.005-Tri	80	VB	25, 13.5	0.005	0.05	38.5	45.67
B80-VC-0.005-Tri	80	VC	25, 8.5	0.005	0.0587	33.5	34.47
B100-VA-0.005-Tri	100	VA	16, 8, 5, 4.5	0.005	0.0511	33.5	41.11
B100-VB-0.005-Tri	100	VB	24, 10.5	0.005	0.05	34.5	42.71
B100-VC-0.005-Tri	100	VC	24, 7.5	0.005	0.0582	31.5	32.72

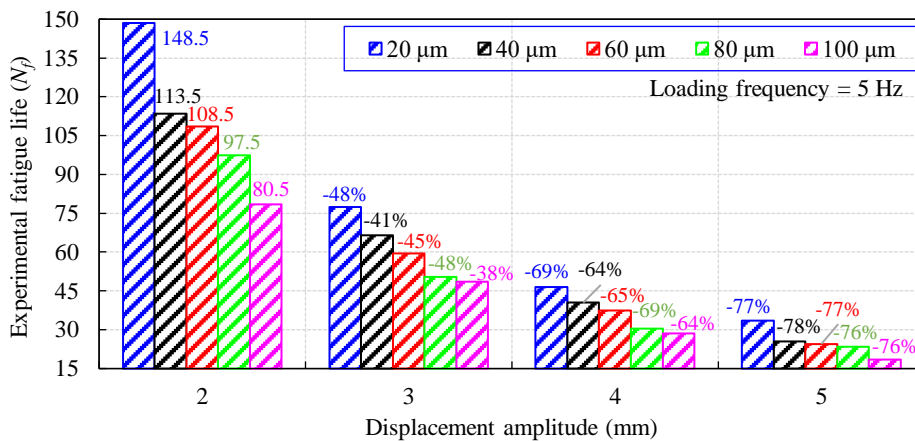
290 Notes: NB, Not blasted; B, blasted; CA, constant loading amplitude; VA, VB, and VC, variable loading amplitude  
 291 patterns;  $R_z$ , surface roughness ( $\mu\text{m}$ );  $d$ , displacement amplitude (mm);  $n_i$ , number of cycles at the  $i^{\text{th}}$  displacement  
 292 amplitude;  $f$ , loading frequency (Hz);  $\Delta\varepsilon$ , average strain range;  $\Delta\varepsilon_{eq}$ , equivalent strain range;  $N_f$ , experimental number  
 293 of cycles to fatigue fracture;  $N_{f,p}$ , predicted fatigue life (cycles)

294 **3 Experimental results and discussions**

295 **3.1 Effect of constant loading amplitude under variable surface roughness on fatigue life**

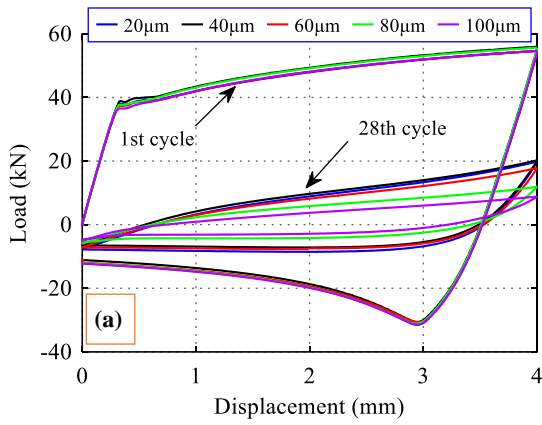
296 This section discusses fatigue life sensitivity to constant loading amplitude of steel with different surface  
297 roughness. A total of 20 ULCF tests for five different roughness were conducted at displacement amplitudes  
298 of 2, 3, 4, and 5 mm and a loading frequency of 0.005 Hz, until the fracture of the test specimens. The  
299 specifications are listed in Table 5. The comparison result of fatigue life as a function of displacement  
300 amplitude and surface roughness is shown in Figure 7, where the numerical values at the amplitude of 2  
301 mm represent the fatigue life  $N_f$ , while at the other displacement amplitudes, the percentage change in  
302 fatigue life is shown. For all roughness levels, a decreasing fatigue life trend was observed when  
303 displacement amplitude increased. At 2 mm, the fatigue life decreased by a factor of 1.89 equivalent to  
304 47%, from 148.5 to 78.5 cycles, when roughness was increased from 20 to 100  $\mu\text{m}$ . At a higher  
305 displacement amplitude of 5 mm, the fatigue life decreased by about 45% from 33.5 to 18.5 cycles with an  
306 increase in surface roughness from 20 to 100  $\mu\text{m}$ . Song et al., (2021a) observed a similar reduction effect  
307 in the ULCF life of steel bridge piers with the increase in corrosion level. In another study by Song et al.,  
308 (2021b), it was investigated that corrosion induced surface roughness has a dominant impact on the ULCF  
309 life of steel specimens. By increasing the corrosion time from 2 to 10 weeks, the average surface roughness  
310 increased by a maximum value of 6.52  $\mu\text{m}$ . Test results indicated that surface roughness increased with the  
311 increase in corrosion level and the ULF fatigue life was decreased by more than 50%. Singh et al., (2019)  
312 presented a novel approach for simulating the effect of three different levels of surface roughness on the  
313 fatigue life of tensile specimens. It is depicted that an increase in the level of surface roughness reduced the  
314 fatigue lives of test specimens. Moreover, at the highest roughness level, the SN curve became steeper  
315 demonstrating that the impact of roughness is more significant at the higher fatigue cycles. McKelvey and  
316 Fatemi, (2012) investigated the fatigue life of generally employed forged steel at various hardness levels  
317 (19HRC, 25 HRC, 35HRC) by conducting rotating bending and reversed cantilever fatigue tests. These

318 studies also pointed out that the surface finish factor is inversely proportional to the number of reversals to  
 319 fatigue failure. This reduction in fatigue life can be explained by the theory of fracture mechanics, the  
 320 increment in the level of surface roughness outcomes in deeper groove marks and smaller radius of bottom  
 321 grains resulting in higher strain concentration, and this process ultimately decreases the resisting capacity  
 322 of the material to fatigue fracture (Wang et al., 2016). Moreover, a 77% reduction in fatigue life was  
 323 observed by increasing the displacement amplitude from 2 to 5 mm for a roughness value of 20  $\mu\text{m}$  as in  
 324 Figure 7. Thus, fatigue life was largely dependent on both loading amplitude and surface roughness, and  
 325 the fatigue life obtained for a smaller roughness was the longest.

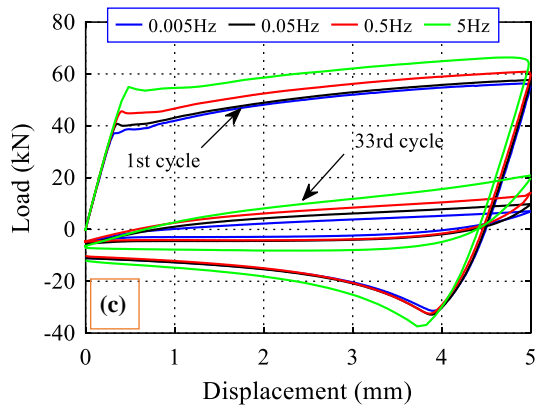
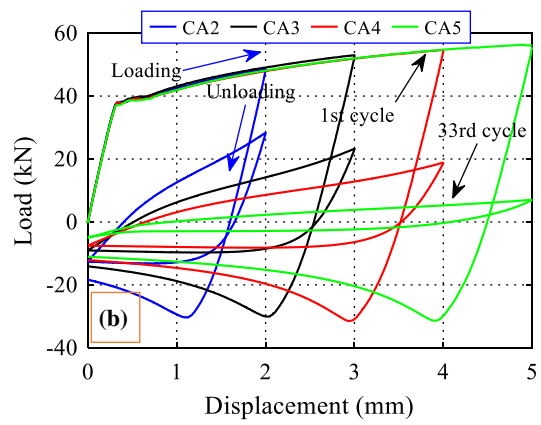


326  
 327 **Figure 7.** Comparison of fatigue life under constant loading amplitudes for different surface roughness  
 328 During the experiments, all specimens experienced local buckling at the mid-height of the specimens after  
 329 surpassing the stage of yield displacement. The occurrence of local buckling caused specimens to deform  
 330 by compression, while visible cracks were observed when the specimens were loaded in tension. Due to  
 331 the application of successive in-elastic loading cycles, the stiffness of the buckled region deteriorated,  
 332 leading to the occurrence of fracture (Salawdeh and Goggins, 2013). A comparative result of the axial load–  
 333 displacement hysteresis loops for the cyclic tests are presented in Figure 8. The result elucidates that for all  
 334 loading conditions, hysteresis response was not identical during the loading and unloading process due to

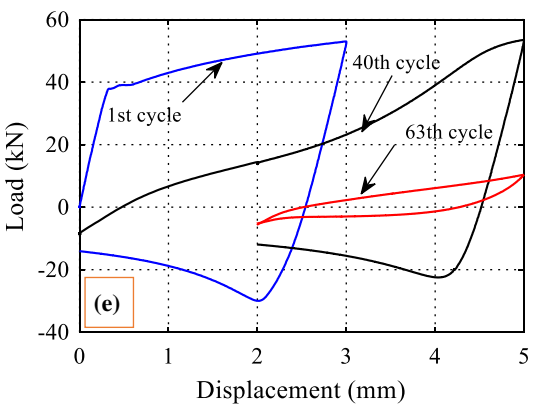
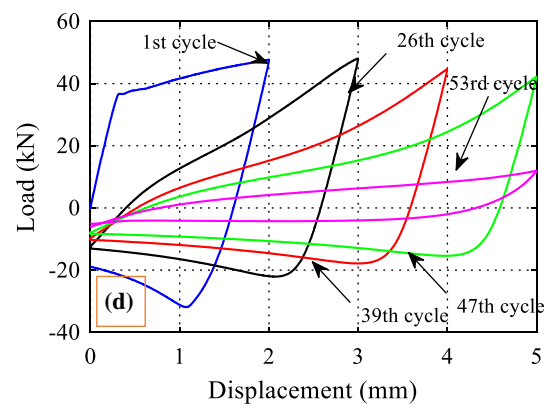
335 the impact of geometrical non-linearity and in-elastic buckling. Moreover, cracks were always formed at  
336 the compression side of the central notch in the specimen during stretching, irrespective of different levels  
337 of roughness and loading conditions. This may have resulted from the high strain generated at the inner  
338 face of the specimen because of the bending deformation of test specimens. To compare the effect of  
339 different surface roughness (20, 40, 60, 80, and 100  $\mu\text{m}$ ) on the ULCF life, load–displacement curves have  
340 been plotted in Figure 8(a) for the case of loading amplitude of 4 mm and loading frequency of 0.005 Hz.  
341 As the fatigue life of 100  $\mu\text{m}$  specimen fatigued at 4 mm amplitude and 0.005 Hz frequency is 28.5 cycles,  
342 so only the 1st and 28th cycles are presented in this figure for the purpose of comparison. These responses  
343 showed that under the similar loading amplitude, the curve area was almost similar at the 1st cycle. However,  
344 at the 28th cycle, the curve area was observed to decrease significantly by 2.81 times as the roughness  
345 varied from 20 to 100  $\mu\text{m}$ . Moreover, since the fatigue experiments were conducted on specimens with  
346 variable surface roughness; however, for the sake of brevity, the hysteresis responses for the 20  $\mu\text{m}$  under  
347 different loading conditions are shown in Figure 8(b to f). The load–displacement curves representing the  
348 effect of a wide range of amplitudes (2, 3, 4, and 5 mm) on the fatigue life of blasted specimens tested at  
349 0.005 Hz are shown in Figure 8(b). For clarity, only the 1st and 33rd cycles results are shown in the figure.  
350 The area of the curve was observed to have increased by 2.85 times, as amplitude varied from 2 to 5 mm  
351 in the 1st cycle. However, the cyclic load degradation was more pronounced at higher amplitudes with the  
352 progressive increase in loading cycles. Finally, in the 33rd cycle, the area of the hysteresis loop drastically  
353 decreased at 5 mm due to the degradation in maximum load carrying capacity as a result of the fracture.  
354 For representing the impact of constant loading amplitude on the ULCF life, dissipation energy, and load  
355 degradation analyses were conducted. Figure 9 illustrates the evolution curves of dissipation energy per  
356 cycle obtained during the complete fatigue tests, for the 20 and 100  $\mu\text{m}$  cases, under various constant  
357 displacement amplitudes. Energy dissipation was evaluated by integrating the area enclosed by the load–  
358 displacement curves and is a crucial parameter for measuring the structural performance under seismic



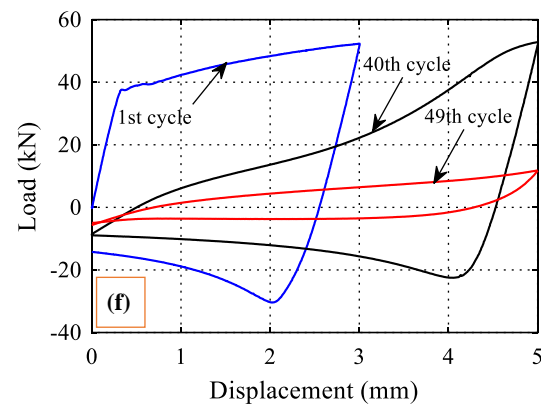
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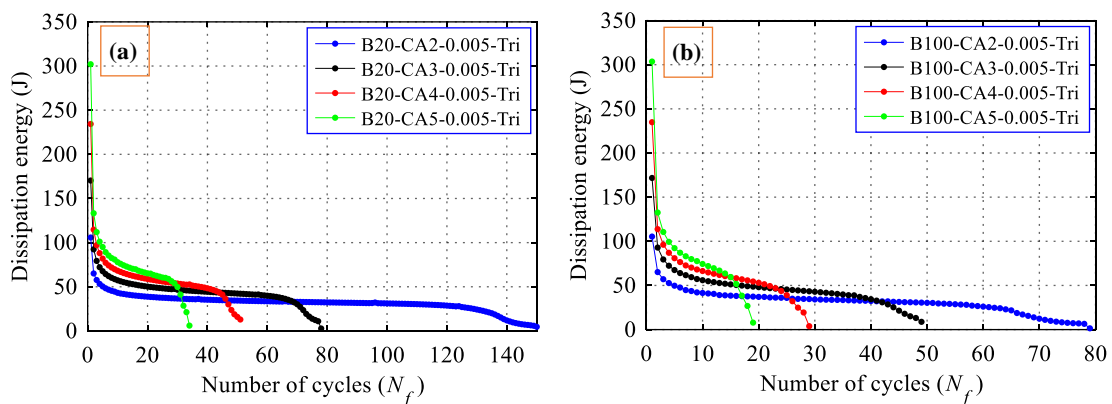


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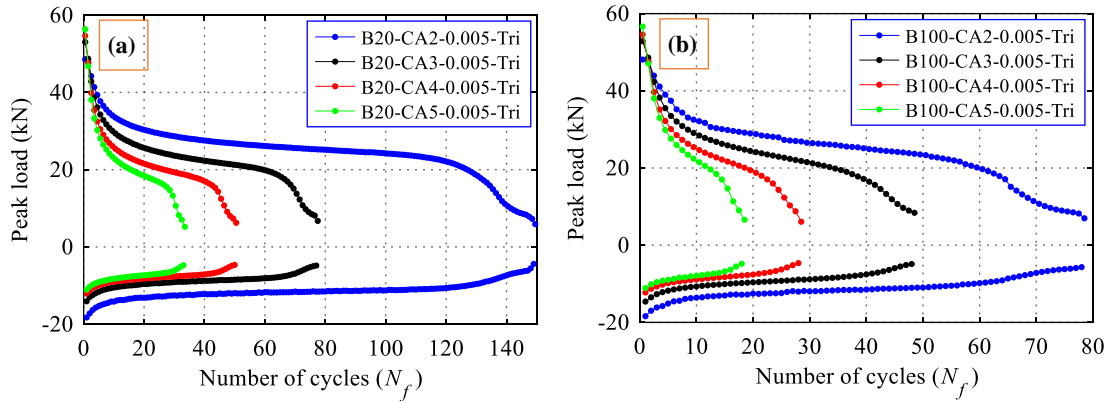


362 **Figure 8.** Hysteresis responses for (a) Specimens with variable surface roughness (b) 20  $\mu\text{m}$  specimens  
 363 under various loading amplitudes, (c) 20  $\mu\text{m}$  specimens under various frequencies, (d) 20  $\mu\text{m}$  specimens  
 364 under pattern VA, (e) 20  $\mu\text{m}$  specimens under pattern VB, and (f) 20  $\mu\text{m}$  specimens under pattern VC

365 loading. From Figure 9, the tendency of energy dissipation was interpreted to be different under various  
 366 loading conditions. At higher amplitudes, peak energy dissipation was observed initially which then  
 367 dropped due to damage accumulation, causing a reduced fatigue life. At the beginning of the fatigue test,  
 368 within the initial loading cycles, energy dissipation decreased remarkably, then stabilized, and finally  
 369 dropped quickly near the state of fracture. Moreover, considering 100  $\mu\text{m}$  rough specimens subjected to 5  
 370 mm loading amplitude, the cumulative energy dissipation (calculated by adding the dissipation energy of  
 371 each cycle) was 1.59 times lower than that for 20  $\mu\text{m}$ , showing a reduction in fatigue life. These results  
 372 indicated that the surface roughness directly affected the energy dissipation capacity of the test specimens.  
 373 The cyclic load response curves for blasted specimens subjected to constant loading amplitude are shown  
 374 in Figure 10. The load values above and below the zero axis represent the peak positive and negative loads  
 375 during loading and unloading stages, respectively. The results implied that load degradation patterns during  
 376 the process of cyclic loading and unloading were almost identical but opposite in directions. However, a  
 377 remarkable difference in the absolute values of peak positive and negative loads existed. On increasing the  
 378 amplitude from 2 to 5 mm, the peak positive loads increased by 1.16 and 1.18 times for 20 and 100  $\mu\text{m}$ ,  
 379 respectively. Moreover, an expedited rate of load degradation specifically for 5 mm loading amplitude  
 380 existed, resulting in lower load range; thus, indicating a decrease in fatigue life at a higher loading amplitude.



381  
 382 **Figure 9.** Influence of various constant loading amplitudes on dissipation energy for (a) 20  $\mu\text{m}$  (b) 100  $\mu\text{m}$



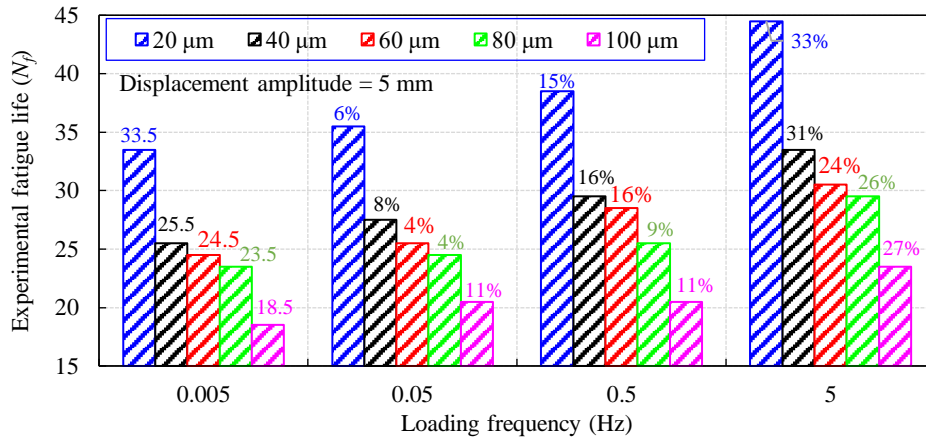
383

384 **Figure 10.** Influence of various constant loading amplitudes on load degradation for (a) 20  $\mu\text{m}$  (b) 100  $\mu\text{m}$

385 **3.2 Effect of loading frequency under variable surface roughness on fatigue life**

386 This section discusses fatigue life sensitivity to the loading frequency of steel with different surface  
 387 roughness. As presented in Table 6, a total of 20 ULCF tests were conducted on blasted specimens at a  
 388 constant displacement amplitude of 5 mm and loading frequencies ranging from 0.005 to 5 Hz. To study  
 389 the effect of loading frequency, combined with surface roughness, on fatigue life, a comparison among  
 390 fatigue life obtained at different loading conditions was performed. The comparison of test results is shown  
 391 in Figure 11, where the numerical values at 0.005 Hz represent the fatigue life  $N_f$ , while at other loading  
 392 frequencies, the percentage change in fatigue life from 0.005 Hz is presented. A decrease in surface  
 393 roughness and an increase in loading frequency led to a significant increase in fatigue life. At 0.005 Hz, the  
 394 fatigue life increased by a factor of 1.81, from 18.5 to 33.5 cycles, with a decrease in surface roughness  
 395 from 100 to 20  $\mu\text{m}$ . At higher loading frequencies of 0.05, 0.5, and 5 Hz, a decrease in surface roughness  
 396 had a similar effect. The results implied that at constant surface roughness, ULCF fatigue life was strongly  
 397 dependent on the loading frequency. Moreover, an increase in loading frequency from 0.005 to 5 Hz  
 398 resulted in a total of 33% increase in fatigue life, for surface roughness of 20  $\mu\text{m}$ . However, the effect was  
 399 less pronounced at higher values of surface roughness.





400

401 **Figure 11.** Comparison of fatigue life under various loading frequencies for different surface roughness

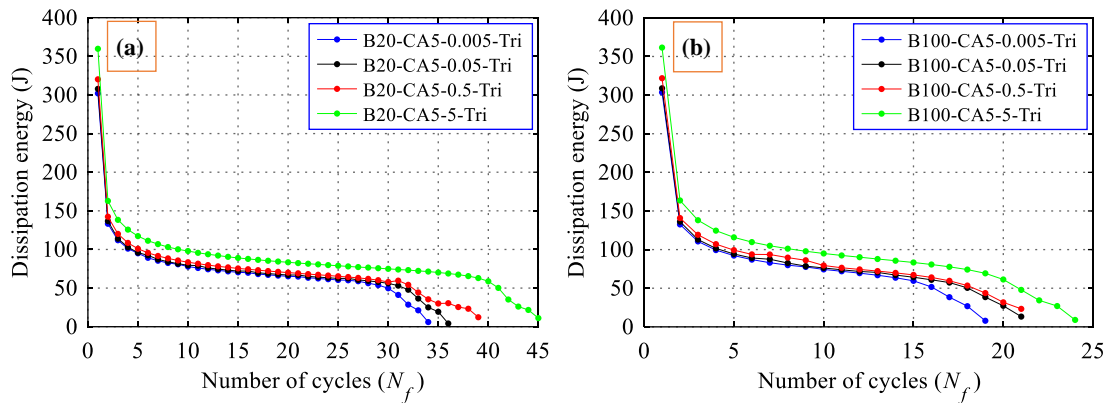
402 This behavior of increment in fatigue life was in agreement with the previous research work (Kanchanomai  
 403 et al., 2003; Reddy et al., 2015a; Luo et al., 2013). In particular, Kanchanomai et al., (2003) conducted LCF  
 404 tests on Sn-Ag eutectic solder at different frequencies ranging from 0.001 to 1 Hz and found that the fatigue  
 405 ductility coefficient increases significantly with increasing frequency. The lower fatigue strength at the  
 406 lower loading rate was attributed to the process of accumulated creep damage under cyclic loading. A  
 407 longer loading time is needed for the experiment conducted at a smaller loading rate resulting in damage  
 408 accumulation and increment in creep damage. Reddy et al., (2015a) investigated the effect of strain rate on  
 409 the LCF life at higher temperatures of 773 and 873 K. The fatigue was observed to increase by around 2.5  
 410 times by increasing the strain rate from  $3 \times 10^{-5}$  to  $3 \times 10^{-3}$ /sec at 773 K. The lower fatigue life at the lower  
 411 loading rate was attributed to the formation of larger stress concentration at the crack tips accounting for  
 412 the increased growth of cracks and reduction in fatigue strength. Moreover, the dominant mechanism  
 413 controlling the deformation and fatigue strength at the higher temperature was identified to be dynamic  
 414 strain gaining. On the other hand, Luo et al., (2013) conducted LCF experiments on high strength structural  
 415 steel in the frequency range of 0.001 to 3 Hz under the total strain range of 2% and concluded that fatigue  
 416 life majorly depends on the loading rate. An increase of about 52% in fatigue life was observed by

417 increasing the loading frequency from 0.001 to 3 Hz. Overall, this increment in fatigue life can be explained  
418 by the fact that with the increase in loading frequency, strain hardening occurs, the temperature rises, and  
419 the material gets less time to recover itself to the original state, which causes an increment in the fatigue  
420 life of the test specimens (Luo et al., 2013).

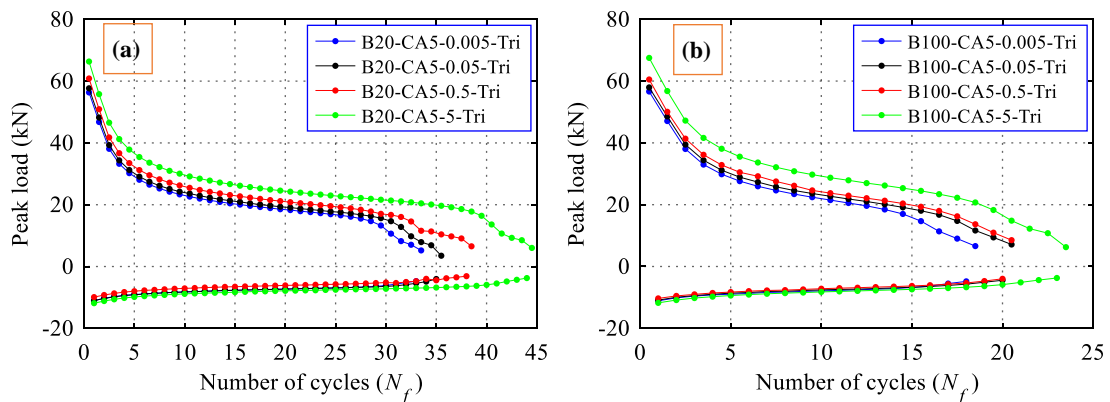
421 Figure 8(c) shows the load–displacement response curves for specimens of roughness 20  $\mu\text{m}$ , tested under  
422 various loading frequencies (0.005, 0.05, 0.5, and 5 Hz) and a constant amplitude of 5 mm. The results for  
423 the 1st and 33rd cycles depicted that the specimens subjected to higher loading frequencies had a steeper  
424 slope of the load–displacement curve as a result of frequency–dependent effect. Subsequently, a large area  
425 of the load–displacement curve represented a larger dissipation energy per cycle. These responses showed  
426 that under the same loading amplitude, the area of the curve increased by 1.19 times with an increase in the  
427 loading frequency, from 0.005 to 5 Hz during the 1st cycle. An increase in peak positive load with the  
428 frequency was also observed; however, this increase in the peak load was not significant from 0.005 to 0.05  
429 Hz. In the 33rd cycle, the area of the hysteresis loop decreased drastically at 0.005 Hz, indicating the failure  
430 of the specimen. Furthermore, the influence of loading frequencies on the ULCF life was evaluated by  
431 analyzing the energy dissipation and load degradation per cycle curves.

432 Figure 12 illustrates the dissipation energy per cycle curves obtained after the complete process of repeated  
433 loading-unloading tests for specimens of roughness 20 and 100  $\mu\text{m}$  under various loading frequencies.  
434 Higher loading frequency had a significant impact on the dissipation energy. Within the initial loading  
435 cycles, the energy dissipated per cycle decreased quickly due to buckling and then stabilized after tens of  
436 loading cycles. Eventually, the dissipation energy suddenly dropped closer to the stage of failure,  
437 accompanied by the fracture of the specimens. Moreover, considering the rough specimens tested at the  
438 frequency of 5 Hz, the cumulative energy dissipated for 100  $\mu\text{m}$  was 1.68 times lesser than that for 20  $\mu\text{m}$ ,  
439 highlighting a reduction in fatigue life.

440 Graphs of cyclic load degradation under variable frequencies for both cases of surface roughness are shown  
 441 in Figure 13. The results highlight that load degradation during the loading and unloading stages was not  
 442 identical and specimens under higher loading frequencies tended to have a late load drop, resulting in higher  
 443 load range. This delay in load drop was an indication of higher fatigue life at a higher frequency. Variation  
 444 in frequency from 0.005 to 5 Hz, increased the peak positive loads by 1.17 and 1.2 times, for 20 and 100  
 445  $\mu\text{m}$ , respectively. Additionally, the fatigue life sensitivity to the variation in loading frequencies was mainly  
 446 reflected by the peak positive loads and not by peak negative loads. Generally, with an increase in frequency,  
 447 a decrease in the final peak positive load is apparently, but the final peak negative load changes slightly.



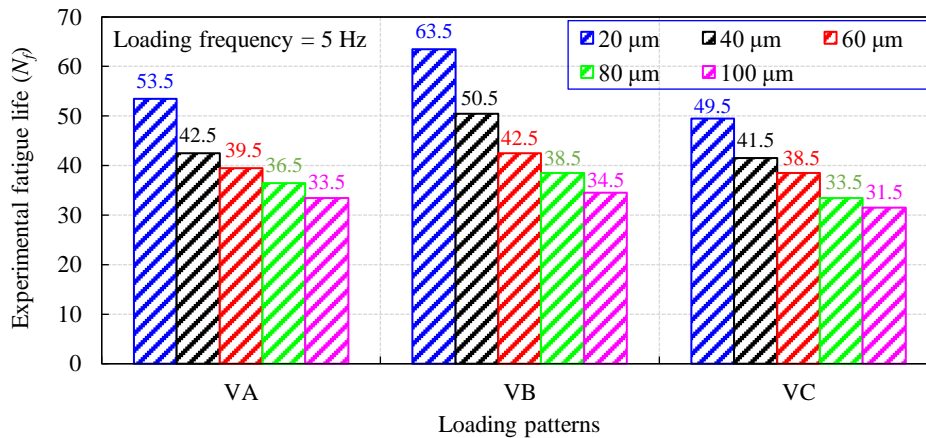
448  
 449 **Figure 12.** Influence of various loading frequencies on dissipation energy for (a) 20  $\mu\text{m}$  and (b) 100  $\mu\text{m}$



450  
 451 **Figure 13.** Influence of various loading frequencies on load degradation for (a) 20  $\mu\text{m}$  and (b) 100  $\mu\text{m}$

452 **3.3 Effect of variable loading amplitude under variable surface roughness on fatigue life**

453 For investigating the effects of variable loading amplitude patterns on fatigue life at different levels of  
454 surface roughness, 15 ULCF tests were conducted at a frequency of 0.005 Hz. Figure 14 elucidates the  
455 dependency of fatigue life on the variable loading patterns for the blasted specimens. Under all levels of  
456 surface roughness, the specimens subjected to loading pattern “VB” had the longest fatigue life relative to  
457 the other two patterns. Therefore, the structures subjected to a loading pattern “VB” with varying mean  
458 loading amplitude were less damaged when compared to four and two-step incremental loading patterns  
459 “VA” and “VC”, respectively. For 20 μm, the fatigue life under pattern “VB” was 1.18 and 1.28 times  
460 higher than that under patterns “VA” and “VC”, respectively. Moreover, the number of cycles of fatigue  
461 life  $N_f$  of specimens subjected to the patterns “VB” and “VC” was lower than that of those tested at a  
462 constant amplitude of 3 mm and higher than those tested at 5 mm.



463

464 **Figure 14.** Comparison of fatigue life under variable loading patterns for different surface roughness

465 Figure 8(d, e, and f) shows the cyclic load–displacement curves of specimens having a surface roughness  
466 of 20 μm subjected to three different loading patterns at a loading frequency of 0.005 Hz. Since all the  
467 loading patterns were different, separate curves were plotted to represent the hysteresis loops after the  
468 application of each incremental loading step. For loading pattern “VA”, the area surrounded by the cyclic

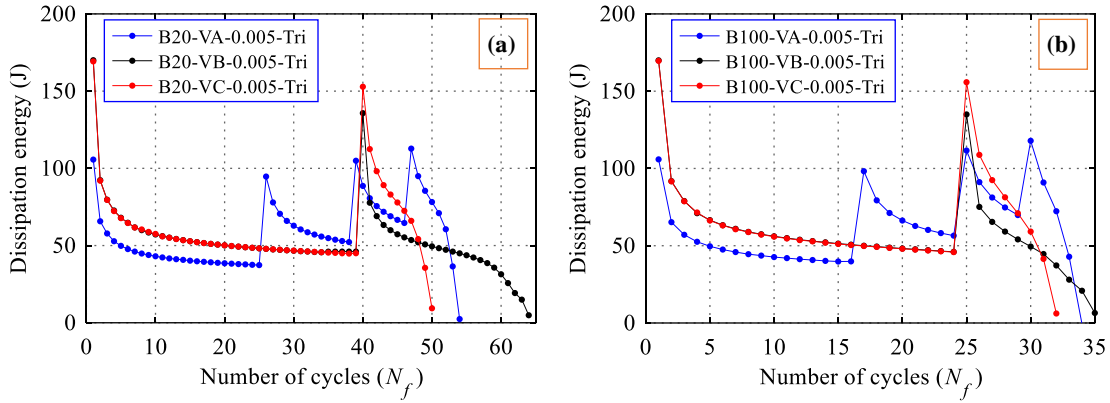
469 curve was observed to have increased after the 2nd loading step, which then decreased after the 3rd and 4th  
470 loading steps. For loading patterns “VB” and “VC”, an increase in the slope and area of the cyclic curve  
471 was observed after the 2nd loading step was applied. The results indicated that the effect of loading pattern  
472 “VC” on the cyclic softening behavior of the steel structures was more significant than that of the other two  
473 patterns, causing a reduction in fatigue life.

474 The evolution energy dissipation curves with the number of cycles under different loading patterns, for  
475 specimens of surface roughness 20 and 100  $\mu\text{m}$  are shown in Figure 15. The dissipation of energy stabilized  
476 after the first few cycles, and then its value changed abruptly when the incremental loading steps were  
477 applied. However, at the last loading step, the dissipation energy was reduced abruptly due to the process  
478 of fatigue damage. Considering the specimens subjected to the “VB” pattern, the cumulative energy  
479 dissipation for 100  $\mu\text{m}$  was 1.66 times lesser than that for 20  $\mu\text{m}$ . In summary, major importance should be  
480 given to energy dissipation capacity for ULCF fatigue occurring under variable loading amplitude.

481 The cyclic load degradation curves for 20 and 100  $\mu\text{m}$  rough specimens subjected to variable loading  
482 patterns are shown in Figure 16. Load degradation during the process of loading and unloading was not  
483 identical and specimens undergoing pattern “VC” tended to have an earlier load drop when compared to  
484 the other two patterns. For pattern “VA”, the peak positive load value increased after the application of the  
485 2nd step of incremental loading and then reduced with the application of the 3rd and 4th steps. However,  
486 for the loading patterns “VB” and “VC,” the peak positive load increased after the application of the 2nd  
487 loading step. The strength reduction was not caused by the displacement applied beyond the ultimate stage  
488 but by the cumulative damage produced under variable loading patterns because of the fatigue phenomenon.

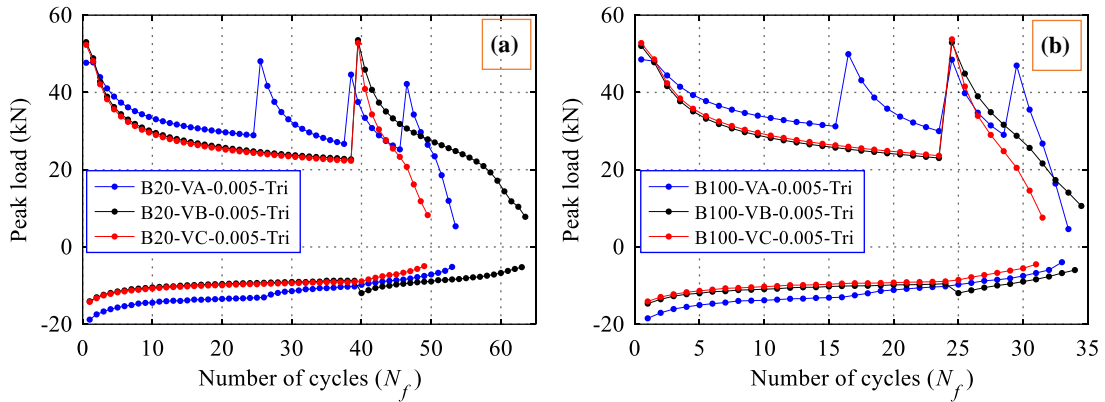
### 489 **3.4 Calculation of strain histories**

490 During the experiment of this study, direct measurement of the strain at the center of the specimen was  
491 challenging because the strain gauges could not be affixed to the observation surface due to buckling, and  
492 the probability of the blasted surfaces getting damaged was high. Since the curvature was localized at the



493

494 **Figure 15.** Influence of variable loading patterns on the dissipation energy for (a) 20  $\mu\text{m}$  and (b) 100  $\mu\text{m}$



495

496 **Figure 16.** Influence of variable loading patterns on load degradation for (a) 20  $\mu\text{m}$  and (b) 100  $\mu\text{m}$

497 at the center of the specimens, a method of strain evaluation, from the curvature of the specimens, using  
 498 the surface height data obtained by laser displacement meter was proposed. Laser scanning was done at the  
 499 compression side of the central notch after every half cycle and then the strain values were evaluated. The  
 500 scanning range is highlighted by a yellow line in Figure 17. Captured surface height points were fitted by  
 501 a polynomial curve (for this study, a sixth-order polynomial was employed). Then, the radius of curvature  
 502 at the bottom of the curve was calculated as described in (Zhao et al., 2021). There was a difference in the  
 503 radius of curvature at the compression and tension sides of test specimens. However, the current research

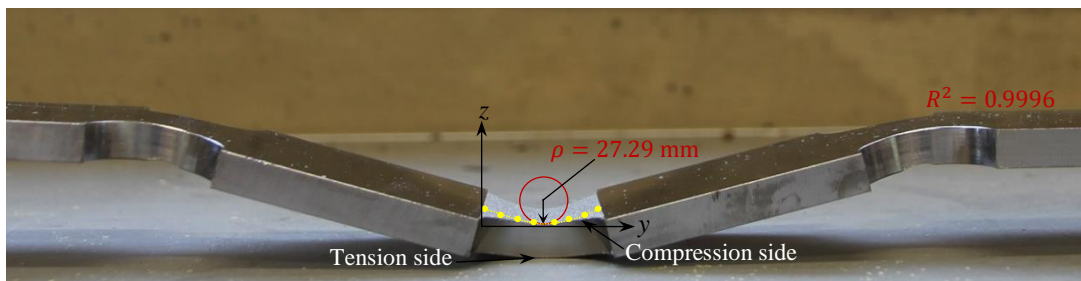
504 work is focused on the fatigue life evaluation of buckling prone steel members undergoing higher bending  
 505 deformation resulting in the generation of maximum strain on the compression side having a smaller radius  
 506 of curvature (Park et al., 2004). Therefore, surface height data was measured only at the compression side  
 507 of the middle notch to evaluate the maximum surface strain. Moreover, the change in thickness was not  
 508 significant, and it was ignored to just consider the effects of surface roughness and loading frequency.  
 509 Finally, after obtaining the radius of curvature, strain values were evaluated using the expressions

$$\rho = \frac{(1 + (z')^2)^{3/2}}{|z''|} \quad (1)$$

$$\varepsilon = -\frac{b}{\rho} \quad (2)$$

510 where  $\rho$  represents the radius of curvature in mm,  $z$  is the surface height (mm),  $\varepsilon$  is the evaluated strain  
 511 value, and  $b$  denotes the distance (mm) from the neutral axis to the surface of the specimen. However, in  
 512 the aforementioned expressions, the effects of Poisson's ratio were ignored. The surface curvature and its  
 513 polynomial fitting curve at 1st loading cycle for B20-CA5-0.005-Tri are shown in Figure 17. The  
 514 corresponding sixth-order polynomial expression is given in equation (3) and the respective  $R^2$  value is  
 515 mentioned in Figure 17.

$$z(y) = 3.06 \times 10^{-8}y^6 - 2.44 \times 10^{-7}y^5 - 3.2 \times 10^{-5}y^4 + 1.01 \times 10^{-4}y^3 + 0.018y^2 - 0.017y + 0.0278 \quad (3)$$



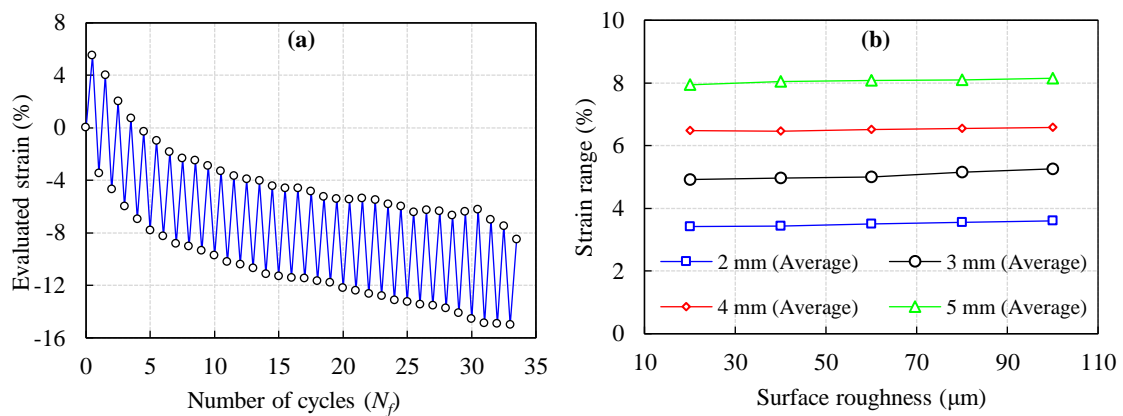
516  
 517 **Figure 17.** Determination of radius of curvature at the center of “B20-CA5-0.005-Tri” from a fitting curve  
 518 at 1st cycle

519 Figure 18(a) illustrates the strain history obtained from the aforementioned method for “B20-CA5-0.005-  
520 Tri”. For out of plane deformation, the strain distribution was non-linear throughout the thickness of the  
521 specimen. Here ‘out of plane’ term refers to the application of load in the longitudinal direction (y-axis) of  
522 the test specimens and the resultant buckling deformation is occurring in the direction of the z-axis of the  
523 specimens. However, the initiation of failure at the surface was probable and developed inwards (Nip et al.,  
524 2010). Moreover, since the surface layer is the most important part during buckling deformation and surface  
525 treatment was also done on it, the surface strain histories were evaluated in this study. These histories were  
526 constructed by calculating the strain values after every half loading cycle. The horizontal and vertical axes  
527 represent the number of half cycles and measured values of strain. Initial axial strain after the first half  
528 cycle was evaluated by the numerical simulation method as adopted by Saleem et al., 2022. Then, this axial  
529 strain was considered in each subsequent strain value. However, this strain would not affect the magnitude  
530 of the average strain range  $\Delta\varepsilon$  employed for the model development as the proposed model is based on  $\Delta\varepsilon$   
531 values which were evaluated by averaging the differences of strain values corresponding to each  
532 consecutive half and full loading cycle. Also, there would not be any effect on the proposed model  
533 parameters. The results revealed that strain at the center of the specimen increased with the progressive  
534 increase in loading cycles, which may be due to the accumulation of residual plastic deformation along  
535 with the progressive development and propagation of cracks.

536 Furthermore, the accuracy of the adopted strain evaluation method from the laser scanning technique was  
537 verified by conducting a numerical simulation (Saleem et al., 2022). In this study, the variation in surface  
538 topography of structural steel with variable surface treatments under fatigue loading was examined, and the  
539 experimentally obtained strain values from the surface curvature method were compared with the numerical  
540 values. Moreover, the main goal of this research is to develop a life prediction model based on large bending  
541 deformation of the test specimens, and this approach is expected to be favorable for the evaluation of larger  
542 bending deformation and large strains (Tateishi et al., 2007). Since the basic Coffin–Manson strain-based



543 model was modified in this study to account for the combined effects of surface roughness, loading  
 544 frequency, and loading amplitude, strain ranges were employed for the development of SN curves. In  
 545 practical applications, strain ranges are calculated from the strain history; thus, evaluations were done using  
 546 the maximum value method described by (Ge and Kang, 2012). Based on strain histories, loading  
 547 amplitudes equal to 2, 3, 4, and 5 mm corresponded to approximately 3.5%, 5%, 6.5%, and 8% average  
 548 strain ranges, respectively, as shown in Figure 18(b). Evaluated average strain range values are reported in  
 549 Table 5, and these were used for the development of the proposed ULCF life prediction model.



550  
 551 **Figure 18.** (a) Strain history of the “B20-CA5-0.005-Tri” specimen (b) Average strain range values for  
 552 different surface roughness

#### 553 4 Development of a new ULCF life prediction model

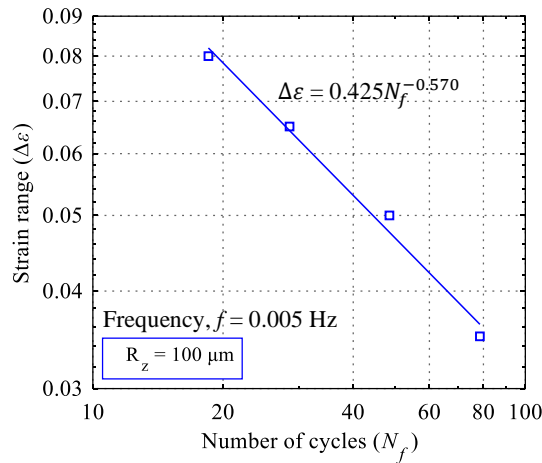
554 While developing the life prediction model, the main challenge was to choose the parameter that was closely  
 555 correlated with the fatigue life. Since the damage to a material is related to its strain deformation, strain-  
 556 based models are commonly used for predicting the LCF life (Tateishi et al., 2007) of metallic materials.  
 557 Thus, the proposed model was also based on strain such that the effects of surface roughness and loading  
 558 frequency on the fatigue life could be considered.

559 **4.1 Basic Coffin–Manson relationship**

560 Considering the wide application of the Coffin–Manson relationship to correlate LCF life and strain range  
561 (Tateishi et al., 2007) through a power law, the basic model was used in this study and formulated as

$$\Delta\varepsilon = c_1 N_f^\alpha \tag{4}$$

562 where  $\Delta\varepsilon$  is the strain range and  $c_1$  and  $\alpha$  are the model parameters. Since plastic strain for the out of plane  
563 deformation was much larger than that in the elastic range, the total strain range was nearly equal to the  
564 plastic strain range, which was directly evaluated using the laser scanning technique. The model parameters  
565 were evaluated by fitting the experimental data of  $\Delta\varepsilon$  versus  $N_f$  (fatigue life) at a given value of surface  
566 roughness and loading frequency (100  $\mu\text{m}$  and 0.005 Hz, in this study). From Figure 19, we observed that  
567 the Coffin–Manson relationship could also correlate to the fatigue life of the considered SM400 steel.



568

569 **Figure 19.** Correlating the strain range and fatigue life of SM400 using the Coffin–Manson relationship  
570 (log-log scale)

571 Table 8 contains the strain life relationships obtained from the present and previous studies  
572 (Sinsamutpadung et al., 2016; Usami et al., 2011) conducted on SM400 steel in the LCF regime. Results  
573 show that the tendency of power law relation fitted by current research agrees with the past research work.

574 The fatigue life of blasted specimens is lower than those of compact tension specimens tested by  
 575 Sinsamutpadung et al., (2016), probably because of the influence of variable loading rate. However, the  
 576 fatigue strength of buckling restrained braces provided in the reference (Usami et al., 2011) tested at the  
 577 almost similar strain range is relatively lower than those of blasted specimens. This might be due to the  
 578 influence of higher buckling mode which develops under the compression phase along with higher stress  
 579 concentration around the welded joints of braces.

580 **Table 8.** Coffin Manson's relationships proposed by different studies

Name	Power law expressions
Present study	$\Delta\varepsilon = 0.425N_f^{-0.570}$
Sinsamutpadung et al., (2016)	$\Delta\varepsilon = 0.793N_f^{-0.451}$
Usami et al., (2011)	$\Delta\varepsilon = 0.210N_f^{-0.488}$

581 **4.2 Characterizing the effect of surface roughness**

582 As summarized in section 3.1, the fatigue life of steel under different surface roughness decreases with the  
 583 increase in loading amplitudes, causing severe damage that leads to the fatigue failure of the steel specimens.  
 584 Thus, the relationship between fatigue life and surface roughness was plotted on a linear scale by power  
 585 fitting the data, as shown in Figure 20, which indicated a negative correlation. The power law function gave  
 586 the best fit to the data set and was expressed as

$$N_f = c_2 R_z^\beta \quad (5)$$

587 Performing the logarithmic operation on equation (5) yielded

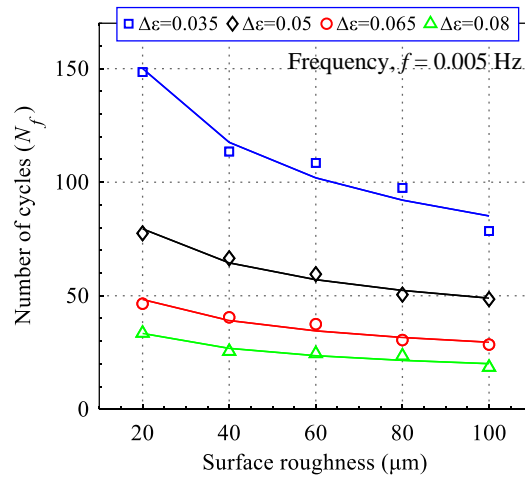
$$\log N_f = \log c_2 + \beta \log R_z \quad (6)$$

588 Thereafter, two important observations were made: ① irrespective of the strain range  $\Delta\varepsilon$ , the fatigue life  
 589  $N_f$  of steel decreased with an increase in surface roughness, confirming the reasonability of considering the  
 590 effect of roughness on fracture in the Coffin–Manson model, and ② the exponents of the fitting lines were

591 very close for different cases of strain ranges, as listed in Table 9. By assuming the exponent to be  
 592 independent of strain range, a relation for characterizing the effect of surface roughness was obtained as

$$\log N_f - \log N_r = \beta \log(R_z/R_{zr}) \quad (7)$$

593 where  $R_{zr}$  is the reference surface roughness, corresponding to the experimental data used for fitting the  
 594 basic model, and  $N_r$  is corresponding reference fatigue life.



595

596 **Figure 20.** Characterizing the effect of surface roughness on the fatigue life (linear scale)

### 597 4.3 Characterizing the effect of loading frequency

598 From section 3.2, the fatigue life was interpreted to increase with an increase in loading frequency under  
 599 different values of surface roughness. Moreover, the fatigue life at the surface roughness of 20 μm was  
 600 higher than that at 100 μm. The relation between loading frequency and fatigue life, illustrated in Figure  
 601 21, indicated a positive correlation. The fatigue life on a logarithmic scale presented a linear correlation  
 602 with the loading frequency. By power fitting the data presented in Figure 21, relevant equations of fitting  
 603 lines were achieved and expressed as

$$N_f = c_3 f^\gamma \quad (8)$$

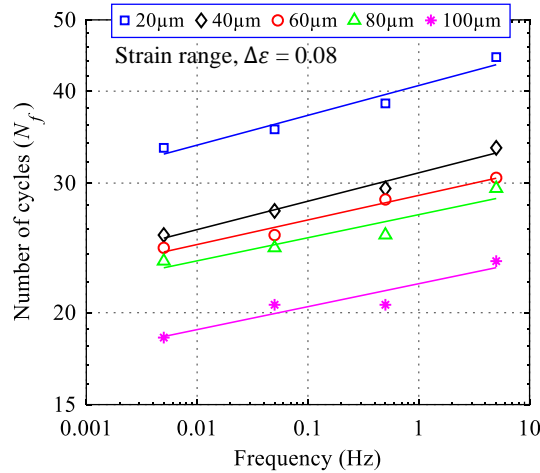
604 Performing the logarithmic operation on equation (8) yielded

$$\log N_f = \log c_3 + \gamma \log f \quad (9)$$

605 From Table 10, we can interpret that the exponents of the equations were close to each other. By considering  
 606 the exponents to be slightly dependent on surface roughness, the change in fatigue life due to variable  
 607 loading frequency was expressed as

$$\log N_f - \log N_r = \gamma \log(f/f_r) \quad (10)$$

608 where  $f_r$  is the reference loading frequency corresponding to the experimental data being used for fitting  
 609 the basic model and  $N_r$  is the corresponding reference fatigue life.



610

611 **Figure 21.** Characterizing the influence of loading frequency on the fatigue life (log-log scale)

#### 612 4.4 Proposed life prediction model

613 In the preceding subsections, equations (4), (7), and (10) were obtained to characterize the impact of strain  
 614 range, surface roughness, and loading frequency, respectively, on fatigue life. This subsection briefly  
 615 discusses an introduction to the newly modified ULCF model. In this paper, reference values of surface  
 616 roughness  $R_{zr}$  and loading frequency  $f_r$  were selected as 100 μm and 0.005 Hz, respectively. Firstly, the

617 fatigue life (denoted as  $N_{ra}$ ) at an arbitrary value of  $\Delta\varepsilon$ , a given frequency  $f_r = 0.005$  Hz, and surface  
 618 roughness  $R_{zr} = 100$   $\mu\text{m}$  was obtained on the basis of equation (4) as

$$N_{ra} = (\Delta\varepsilon/c_1)^{1/\alpha} \quad (11)$$

619 Performing the logarithmic operation on equation (11) yielded

$$\log N_{ra} = 1/\alpha(\log (\Delta\varepsilon/c_1)) \quad (12)$$

620 Thus, when the value of  $R_{zr}$  in equation (7) was fixed to 100  $\mu\text{m}$ ,  $N_r$  in equation (7) was actually equal to  
 621  $N_{ra}$ . Substituting  $N_{ra}$  as  $N_r$  in equation (7), the fatigue life (denoted by  $N_{rb}$ ) at an arbitrary value of  $\Delta\varepsilon$  and  
 622  $R_z$  for a given  $f_r$  was expressed as

$$\log N_{rb} - \log N_{ra} = \beta \log(R_z/R_{zr}) \quad (13)$$

$$\log N_{rb} = 1/\alpha(\log (\Delta\varepsilon/c_1)) + \beta \log(R_z/R_{zr}) \quad (14)$$

623 Similarly, after fixing  $f_r = 0.005$  Hz in equation (14),  $N_r$  in equation (10) was replaced by  $N_{rb}$ . Thereafter,  
 624 substituting  $N_{rb}$  as  $N_r$  in Eq. (10), a new ULCF life prediction model incorporating the effects of strain  
 625 range, surface roughness, and loading frequency was expressed as

$$\log N_f - \log N_{rb} = \gamma \log(f/f_r) \quad (15)$$

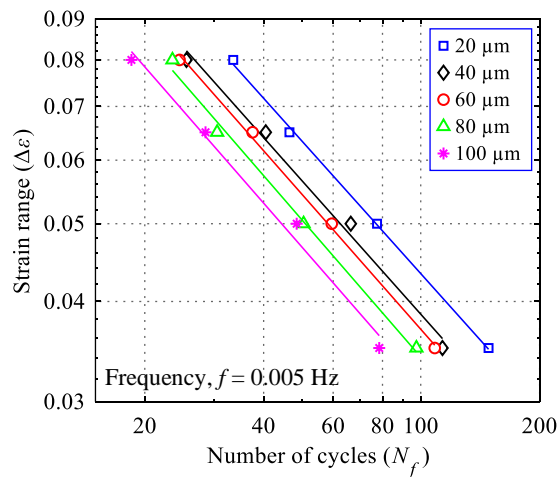
$$\log N_f = 1/\alpha(\log (\Delta\varepsilon/c_1)) + \beta \log(R_z/R_{zr}) + \gamma \log(f/f_r) \quad (16)$$

626 where  $\Delta\varepsilon$ ,  $R_z$ , and  $f$  are the strain range, surface roughness, and loading frequency, respectively;  $R_{zr} = 100$   
 627  $\mu\text{m}$  and  $f_r = 0.005$  Hz are the reference surface roughness and loading frequency, respectively, determined  
 628 by fitting the corresponding data; and  $c_1$ ,  $\alpha$ ,  $\beta$ , and  $\gamma$  are the model parameters which are listed in Table 11.  
 629 The model parameters  $\beta$  and  $\gamma$  were taken as the average slopes of the fitting lines as shown in Figures 20  
 630 and 21, respectively.

631 **5 Model validation**

632 Since the proposed fatigue life prediction model is purely empirical, its reliability must be validated through  
633 comprehensive experimental results. To verify its prediction accuracy, the proposed model was applied to  
634 all the test data listed in Tables 5, 6, and 7. Specifically, the validity of the proposed model was checked by  
635 applying the model to an unknown test dataset (not used for the development of the model) listed in Table  
636 7. The specimens in this data set were tested under variable loading amplitude because real engineering  
637 structures experience cycles of variable amplitudes during their service life. The simplified fatigue life  
638 model as expressed by equation (4) was fitted to the experimental test results of steel specimen with variable  
639 surface roughness presented in Table 5, tested at constant loading amplitudes under a loading frequency of  
640 0.005 Hz, for plotting the S-N curves shown in Figure 22. The parameters of the basic Coffin–Manson  
641 equation at five different roughness were extracted by performing linear regression analysis and the  
642 corresponding coefficients are summarized in Table 12.

643



644

645 **Figure 22.** S-N Curves of SM400 using the Coffin–Manson relationship at different surface roughness

646 (log-log scale)

647

648 **Table 9.** Coefficient  $c_2$  and exponent  $\beta$  at four different strain ranges with  $f = 0.005$  Hz

Coef.	Strain range, $\Delta\varepsilon$			
	0.035	0.05	0.065	0.08
$c_2$	430.70	195.75	120.90	86.10
$\beta$	-0.352	-0.301	-0.306	-0.316
$R^2$	0.949	0.970	0.926	0.924

649 **Table 10.** Coefficient  $c_3$  and exponent  $\gamma$  at five different roughness with  $\Delta\varepsilon = 0.08$

Coef.	Surface roughness, $R_z$ ( $\mu\text{m}$ )				
	20	40	60	80	100
$c_3$	40.71	30.98	28.87	27.18	21.89
$\gamma$	0.0405	0.0386	0.0334	0.0314	0.0312
$R^2$	0.9657	0.977	0.975	0.889	0.890

650 **Table 11.** Proposed model parameters

Model	$c_1$	$\alpha$	$\beta$	$\gamma$
parameters	0.425	-0.570	-0.3035	0.03502

651 **Table 12.** Coefficient  $c_4$  and exponent  $\eta$  at five different roughness

Coef.	Surface roughness, $R_z$ ( $\mu\text{m}$ )				
	20	40	60	80	100
$c_4$	0.543	0.492	0.484	0.466	0.425
$\eta$	-0.549	-0.553	-0.559	-0.568	-0.570
$R^2$	0.998	0.992	0.997	0.991	0.992

652 Existing studies have indicated that Miner's rule results in an overestimation of fatigue life in the ULCF  
653 regime (Tateishi et al., 2007; Xue, 2008). Nevertheless, Miner's rule still gives accurate results when the  
654 largest applied strain range  $\Delta\varepsilon$  is lesser than the damage strain threshold. True strain at the point of  
655 maximum tensile stress has been recommended as the damage strain threshold (Tateishi et al., 2007). In  
656 this study, the largest strain was 8% (Figure 18(b)), which was lesser than approximately 25% of the damage



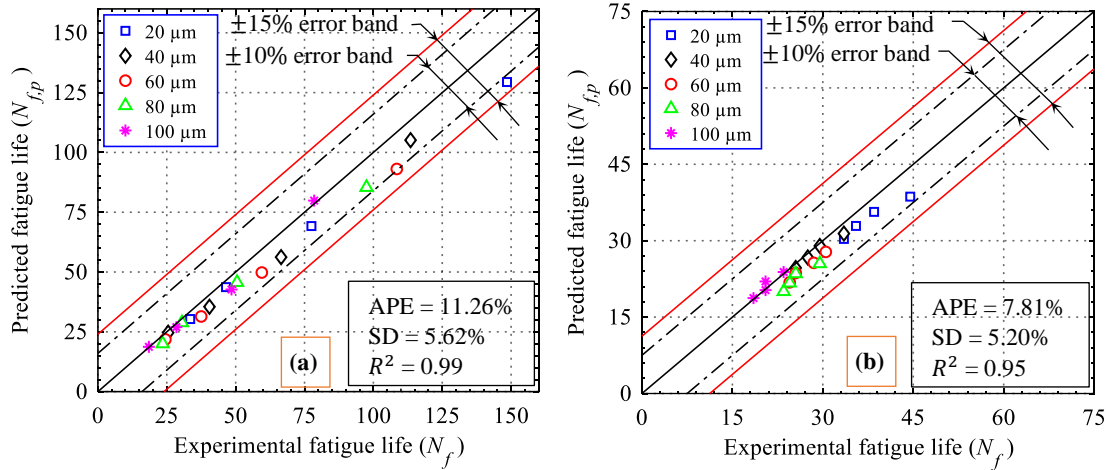
657 threshold value determined by conducting tension tests (Figure 1(b)). Accordingly, Miner's rule can be  
 658 employed in this research study without any modification for the calculation of the equivalent strain range  
 659 in the ULCF regime (Dehghani et al., 2017). The equivalent strain ranges under variable loading amplitude  
 660 for each roughness case were expressed as (Tateishi et al., 2007)

$$\Delta\varepsilon_{eq} = \left( \frac{\sum(\Delta\varepsilon_i^{1/\eta} \cdot n_i)}{N_f} \right)^\eta \quad (17)$$

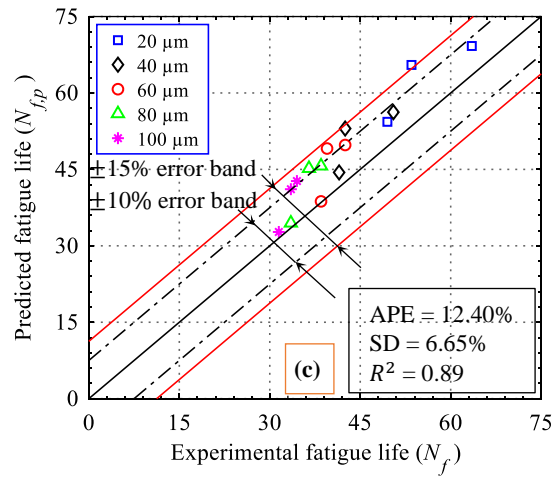
$$N_f = \sum n_i \quad (18)$$

661 where  $\Delta\varepsilon_{eq}$  is the equivalent strain range,  $\eta$  is the material constant, and  $n_i$  represents the number of  
 662 loading cycles for the  $i$ th strain range. The calculated equivalent strain ranges are listed in Table 7. By using  
 663 the calculated values, the fatigue life under variable loading amplitudes of all the blasted specimens in this  
 664 group was predicted.

665 Figure 23 illustrates the comparison between experimental fatigue life  $N_f$  and predicted fatigue life  $N_{f,p}$  of  
 666 all the test specimens. The black dashed and solid red lines represent the  $\pm 10\%$  and  $\pm 15\%$  error bands,  
 667 respectively. The efficacy of the proposed model for fatigue life estimation was estimated based on the  
 668 percentage error (PE) calculated as  $PE = 1 - |N_{f,p} - N_f| / N_{f,p}$  (Dehghani et al., 2017). Statistics of the  
 669 percentage error provided information on the effectiveness of fatigue life estimation. Furthermore, average  
 670 value (APE) and standard deviation (SD) of the PE were evaluated and highlighted in Figure 23 for each  
 671 data set. In the case of specimens tested under constant loading amplitude with variable surface roughness  
 672 as shown in Figure 23(a), out of a total of 20 data points, 19 points (95% data) were located within a  $\pm 10\%$   
 673 error band, while only 1 point fell in the  $\pm 15\%$  error band. A majority of the data points were below or  
 674 close to the ideal regression line of  $45^\circ$ . Moreover, the APE and SD were 11.26% and 5.62%, respectively.  
 675 Considering the effects of variable frequency on the ULCF life as shown in Figure 23(b), all 20 points  
 676 (100% data) for five different cases of roughness were located within an error band of  $\pm 10\%$ . For this



677



678

679 **Figure 23.** Comparison of the experimental and predicted fatigue life obtained using the proposed model  
 680 (linear scale) under (a) constant loading amplitude, (b) loading frequency, and (c) variable loading  
 681 amplitude  
 682 case, the calculated values of APE and SD were 7.81% and 5.20%, respectively, providing satisfactory  
 683 results. The error between experimental and theoretical fatigue life for this data set ranged between 0.99 to  
 684 17.38%. Figure 23(c) presents the results of specimens under different variable loading amplitude patterns.  
 685 Out of 15 points, 10 points were within the  $\pm 10\%$  error band, 4 points fell inside an error band of  $\pm 15\%$ ,

686 and only 1 point was outside the  $\pm 15\%$  error band. Under variable loading amplitude, 93% of data (14 data  
687 points) of the predicted fatigue life for the tested specimens were within an acceptable error band of  $\pm 15\%$ .  
688 Thus, the results showed that the proposed model was capable of predicting fatigue life in the case of  
689 variable loading patterns with reasonable accuracy. Considering the overall data set containing 55  
690 specimens with variable surface roughness, 89% of data were within the  $\pm 10\%$  error band; 9% of data  
691 fitted inside the  $\pm 15\%$  error band; and only 2% of data fell outside the  $\pm 15\%$  error band, indicating the  
692 efficacy of the proposed model.

693 The proposed model comprising of equation (16) can be applied to the buckling prone structural members  
694 made up of SM400 steel such as lateral and sway bracings, vertical stiffeners, I-section girders, pipes, and  
695 piers with the similar condition of experimental specimens of this study. On the other hand, SM400 is one  
696 of the most commonly used structural steels in Japan. In order to clarify the generality of the model, further  
697 study targeting a wide range of steels and structural components is desirable.

## 698 **6 Conclusions**

699 In this study, a total of 59 displacement-controlled tests were conducted to study the effects of surface  
700 roughness, loading amplitudes, and loading frequencies on the fatigue life of SM400 structural steel in the  
701 ULCF regime. Based on the conventional fatigue theory and experimental data, a new mathematical model  
702 accounting for the combined effect of the aforementioned parameters is proposed. The model parameters  
703 are estimated by fitting the experimentally obtained data. Finally, variable and constant amplitude test  
704 results are used to validate the accuracy of the proposed model. The main conclusions of this study are  
705 summarized as follows:

- 706 1. The combined effects of surface roughness and loading amplitude have a significant impact on the  
707 ULCF life of structural steel. An increase in surface roughness and loading amplitude resulted in the  
708 acceleration of fatigue damage and earlier failure of steel specimens, which became more distinct at  
709 higher values. An increase in loading amplitude from 2 to 5 mm resulted in a 77% decrease in the

710 ULCF life for specimens of surface roughness 20  $\mu\text{m}$ . On studying the effect of surface roughness,  
711 fatigue life was observed to decrease significantly by a factor of 1.89, from 148.5 to 78.5 cycles, with  
712 an increase in surface roughness from 20 to 100  $\mu\text{m}$  at a loading amplitude of 2 mm.

713 2. From the experimental results, the ULCF life of the specimens was found to be evidently sensitive to  
714 variations in loading frequency. An increase in loading frequency from 0.005 to 5 Hz caused an  
715 increase of 33% in the fatigue life of specimens with 20  $\mu\text{m}$  surface roughness. Additionally, on  
716 evaluating the impact of surface roughness, the fatigue life was observed to increase by a factor of 1.81,  
717 from 18.5 to 33.5 cycles, with a decrease in the surface roughness, from 100 to 20  $\mu\text{m}$  at the loading  
718 frequency of 0.005 Hz. In addition, results demonstrated that the effects of loading amplitude on fatigue  
719 life were larger than those of loading frequency under a specified value of surface roughness.

720 3. Loading conditions have a substantial effect on the ULCF behavior of specimens. Blasted specimens  
721 subjected to higher loading frequency showed higher energy dissipation and late drop in peak load,  
722 indicating longer fatigue life. While those subjected to higher loading amplitude presented lower  
723 energy dissipation and earlier drop in peak load, highlighting a reduction in fatigue life.

724 4. A new ULCF life prediction model is proposed, which establishes a relation between the parameters  
725 of surface roughness, loading amplitude, loading frequency, and fatigue life. The predicted results  
726 corroborated well with the experimental data on the suitable selection of the model parameters. The  
727 analysis results showed that the predicted life for almost all the data was within an acceptable error  
728 band of  $\pm 15\%$ , while  $R^2$  ranged from 0.89 – 0.99, representing the effectiveness of the proposed model.

729 To summarize, this study demonstrates the combined effects of surface roughness, loading frequency, and  
730 loading amplitude on the fatigue life of metal structures. The introduction of these parameters into the  
731 ULCF life estimation model extends its usefulness in various engineering applications whereby surface  
732 treatment of structures is indispensable. Thus, the proposed model is expected to assist structural engineers  
733 and researchers at the design and maintenance stages to accurately calculate the ULCF life and to prevent

734 associated fatigue failures. This study can be further extended to future research to account for the effects  
735 of (1) other loading waveforms such as sinusoidal etc., (2) other specimen geometry such as thickness,  
736 width, length, etc., and (3) other types of steels on ULCF life.

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